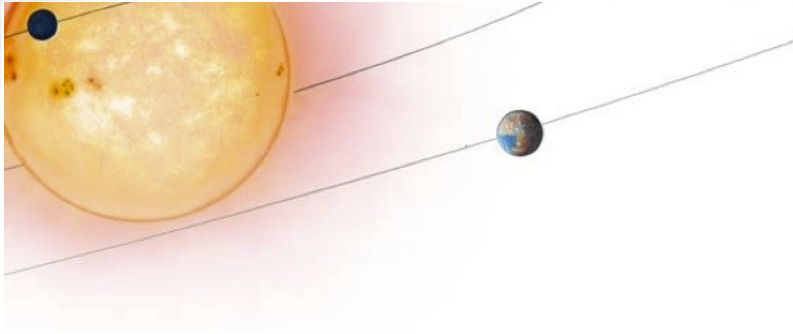


# PLATO: instrument performance

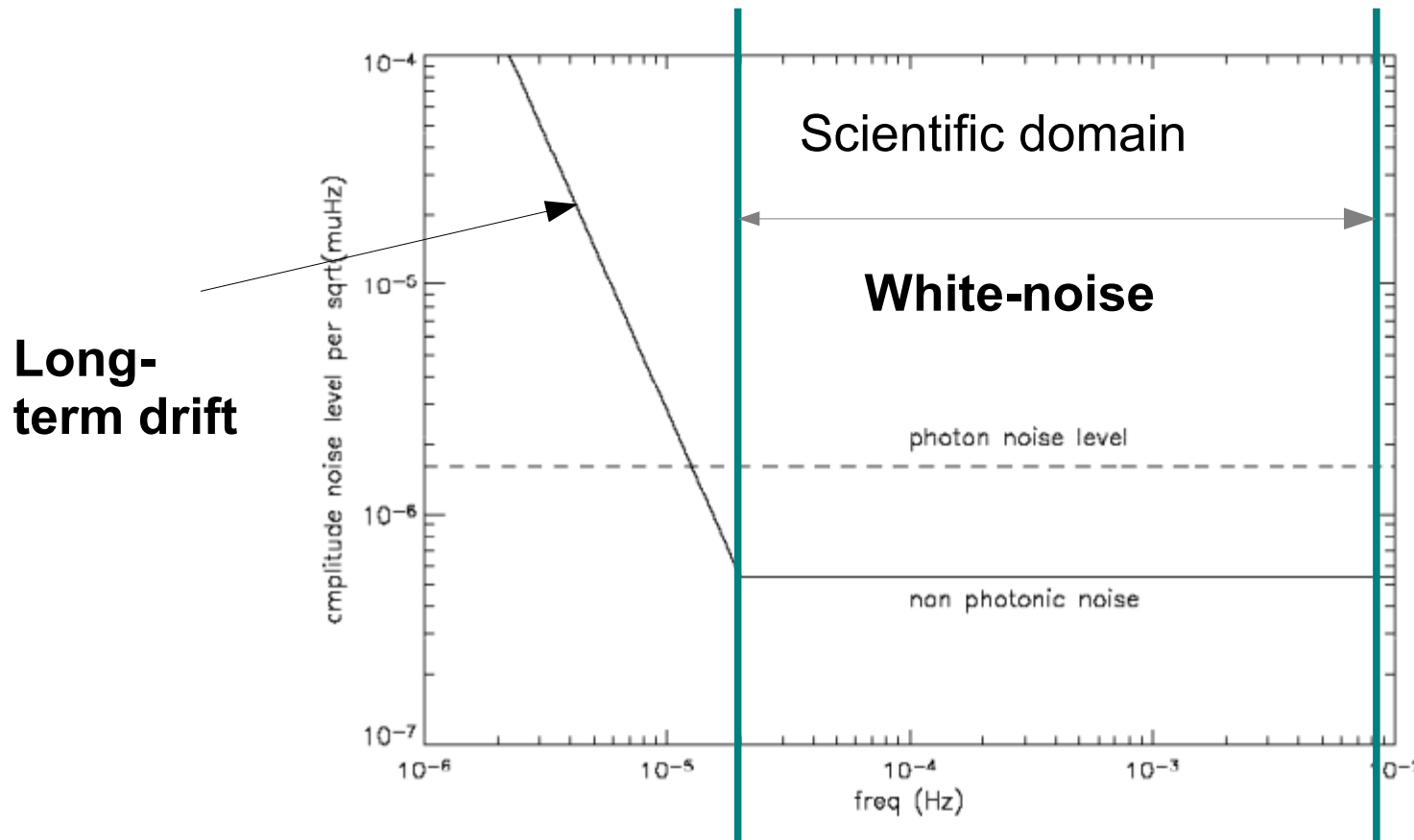
- 1) Noise level requirements
- 2) Expected white noise level
- 3) Long-term drift



# PLATO: instrument performance

- 1) **Noise level requirements**
- 2) Expected white noise level
- 3) Long-term drift

# Noise level requirements



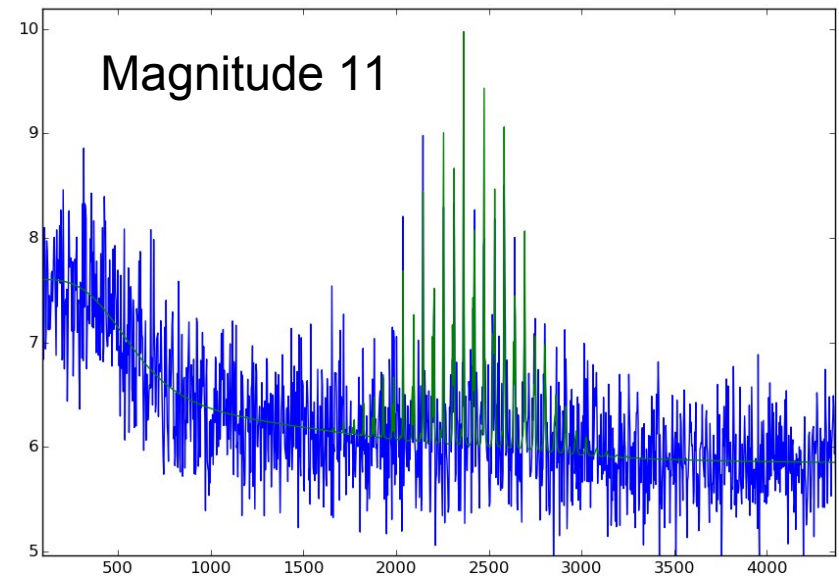
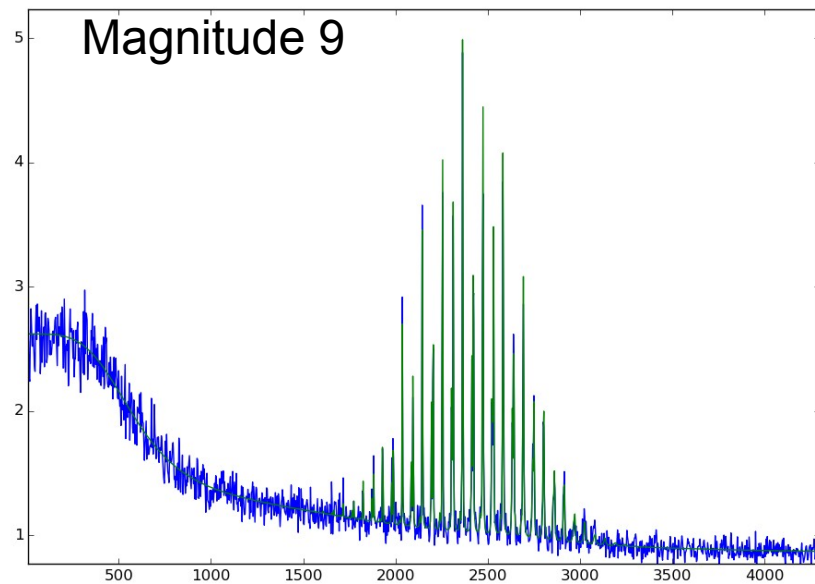
Non photonic noise requirements for stars with  $m_v = 11$  : **1/3 of the photon noise** in *total*

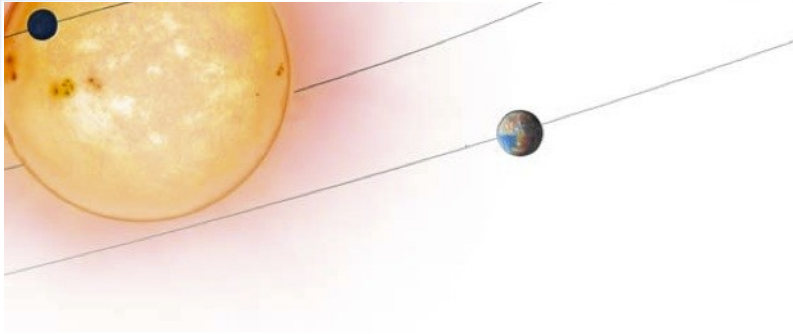
# Noise level requirements

Reference noise level for 32 telescopes at V=11 :

- Photon noise 27 ppm in 1 hr
- Non-photonic noise = photon noise / 3
- Total : **28.5 ppm in 1 hr**

Light-curve of a MS solar-like pulsator simulated with the Stellar Light-curve Simulator (**SLS**)





# PLATO: instrument performance

- 1) Noise level requirements
- 2) **Expected white noise level**
- 3) Long-term drift

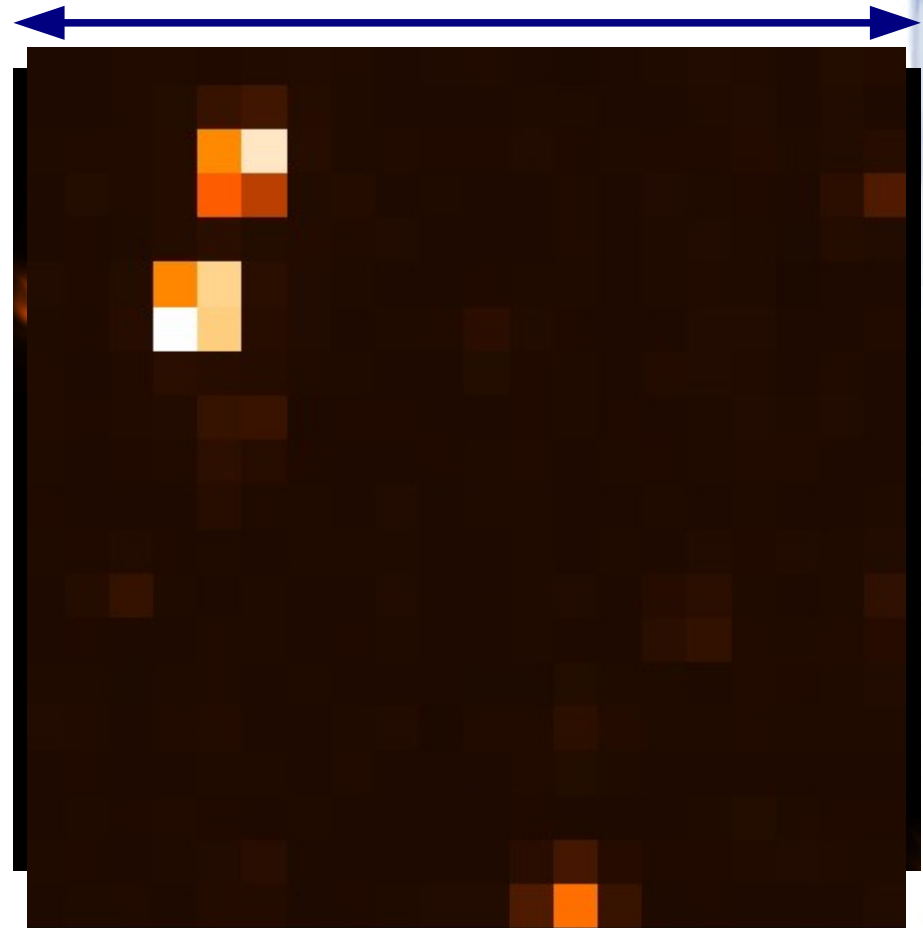
# Simulations of imager time-series

- Time-series of imagerettes of size 20 x 20 pixels generated with the **Plato Image Simulator (PIS)** developed at LESIA

- PRNU (3%)
- Read-out noise
- **Satellite jitter:**
  - Compliant with the specifications
  - Uncorrelated between telescopes
- Long-term effects *neglected* (e.g. differential aberration)

- ➔ PSF : optical design from March 2011
- ➔ Extend and complete the Phase A assessment study (PLATO-GS-TN-235-LESIA)

20 x 20 pixels  
Resolution : 1/128 pixels



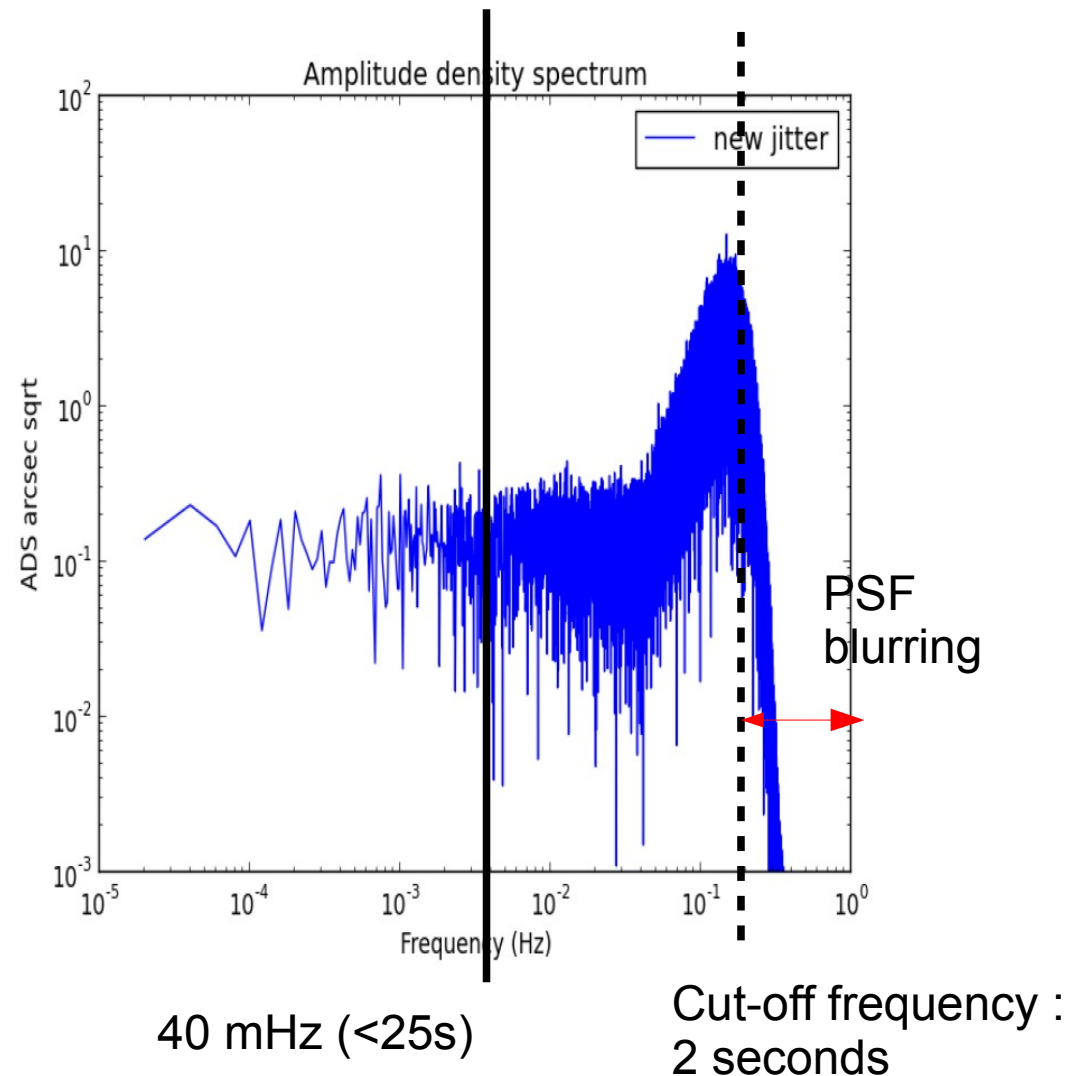


# Requirements in terms of pointing errors

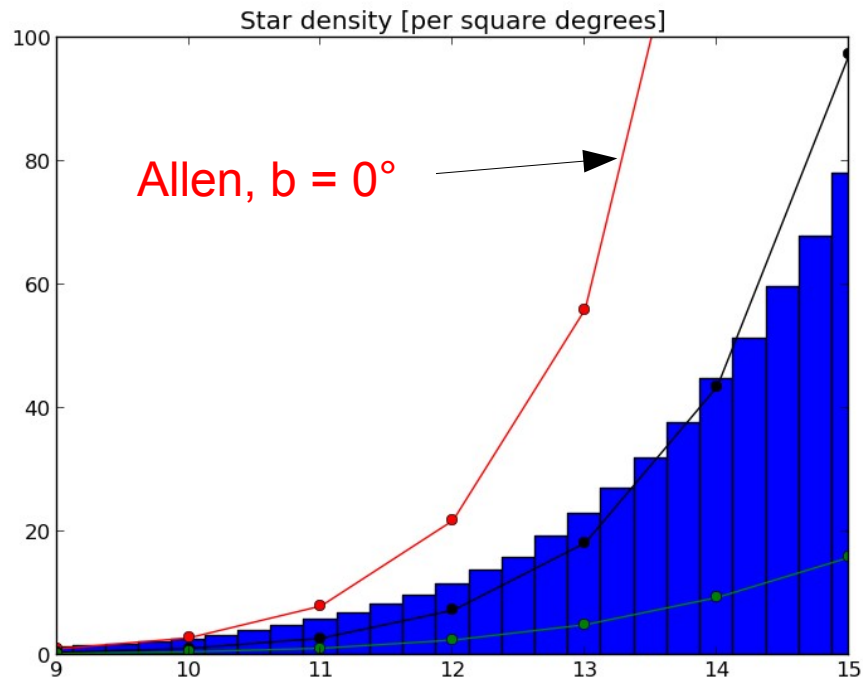
## Pointing requirements

- Below 40 mHz (>25s) :
  - ➔ Flat in the frequency domain
  - ➔  $0.23''/\sqrt{\text{Hz}}$
- Above 40 mHz (<25s) :
  - ➔ In the time domain
  - ➔ 3" at 95 % confidence level
  - ➔  $\sim 1.5'' \text{ rms} = 0.1 \text{ pixels rms}$

See PLATO Pointing Requirements Definition Document, SRE-PA/2010.065, Issue 2, Rev. 0



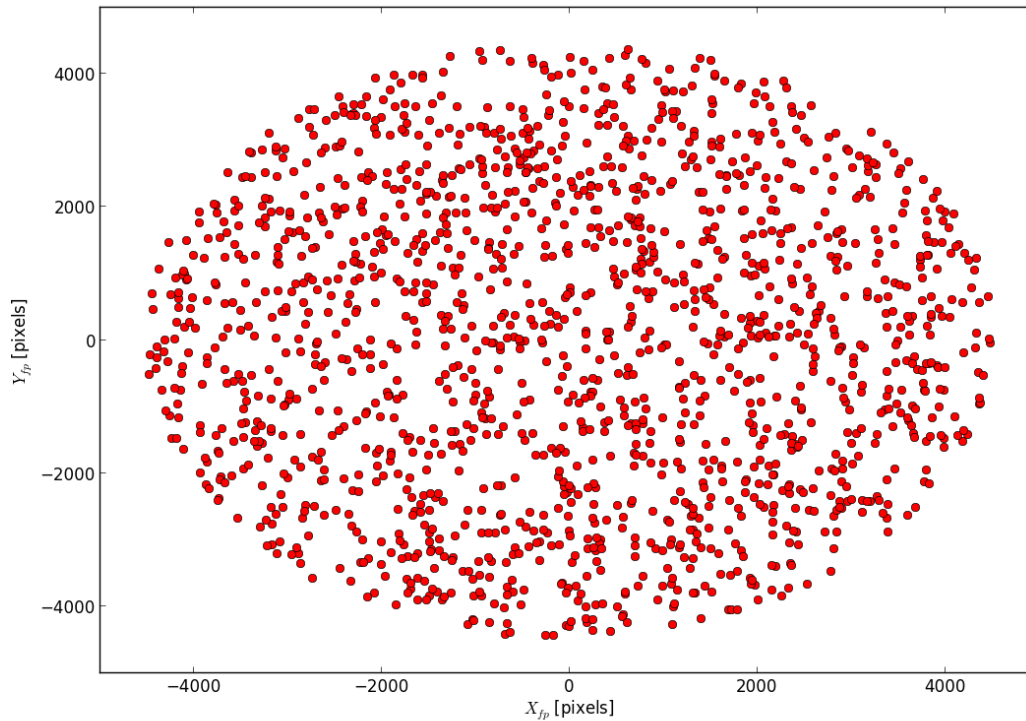
# Stellar field



- Synthetic stellar population model (Besançon model)
- Galactic latitude :  $-30^\circ$ ,  $l = 253^\circ$  (first proposed pointing direction)
- Size : 300 sq. degrees
- Up to magnitude 18

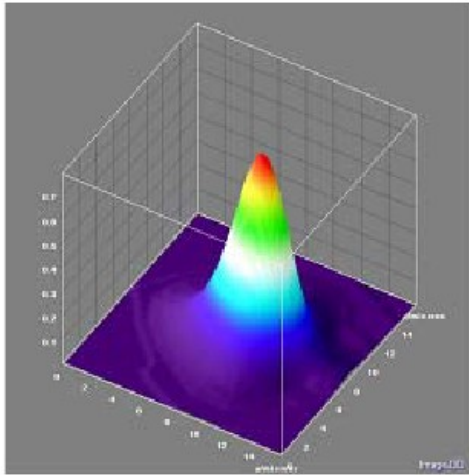


# Field of view

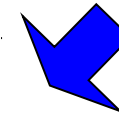
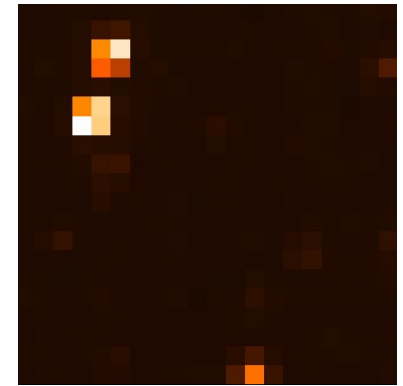
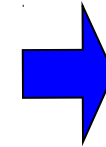
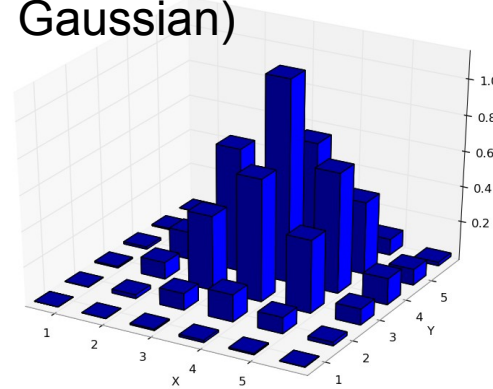
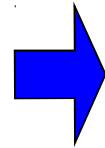


- Normal Telescope (group 1) → not aligned with the Fast Telescopes
- About **1 500 imagerettes** centred around stars between  $V= 9$  and  $V = 13$

# Weighted mask based photometry



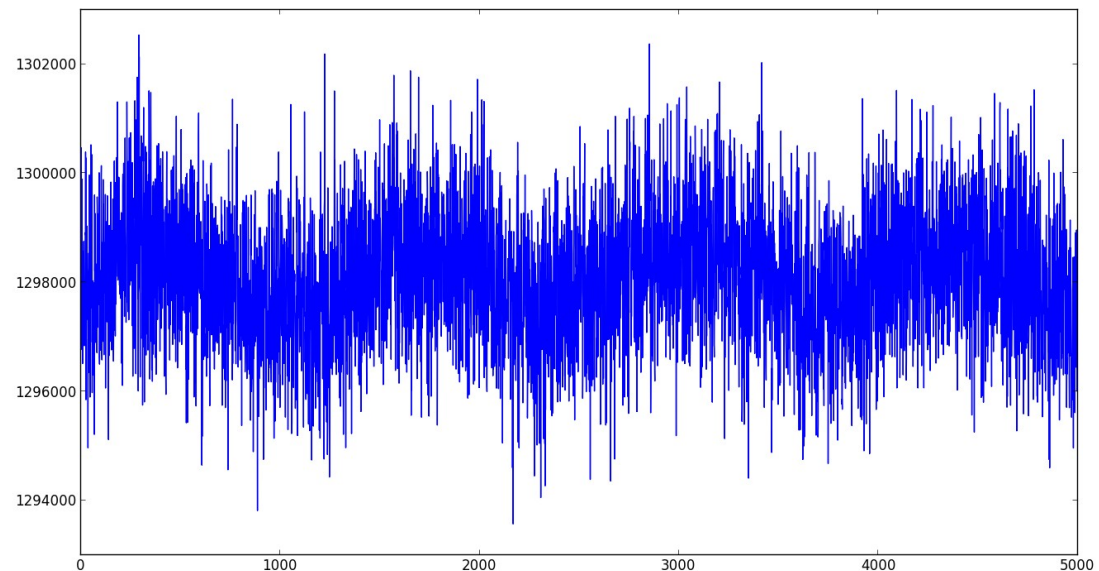
weighted mask  
(e.g. Gaussian)



Mask width :

$$\delta(\theta) = 1 + \frac{1}{2} \left( \frac{\theta}{14.14} \right)$$

Computed light-  
curve :

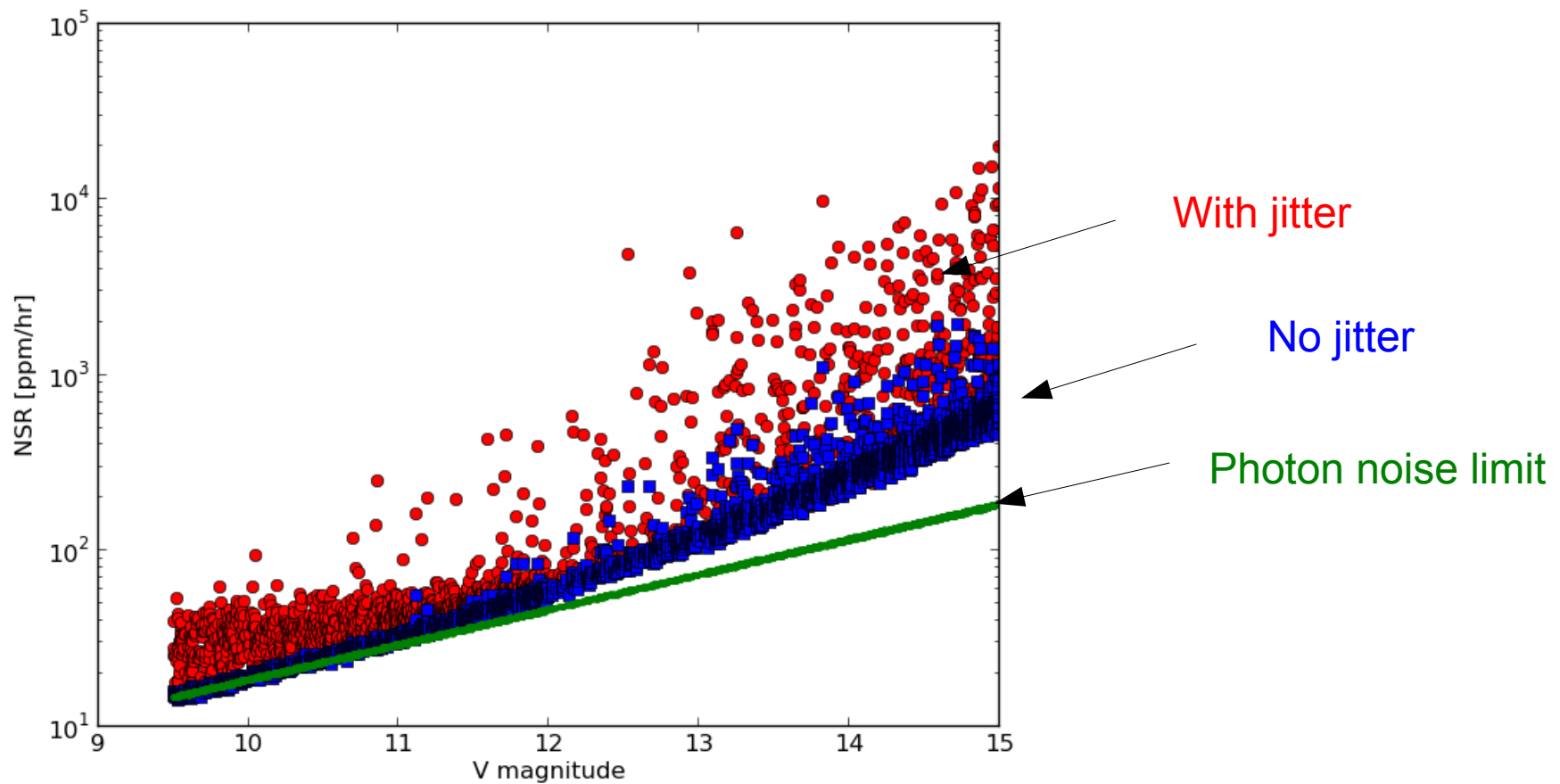


# Raw results

$$NSR = 10^6 \sqrt{\frac{2\Delta T}{3600n} \frac{\sigma}{\bar{s}}}$$

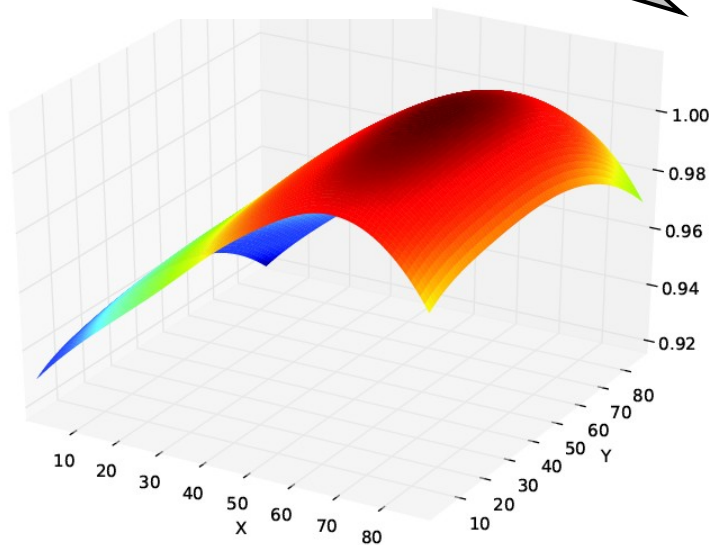
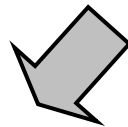
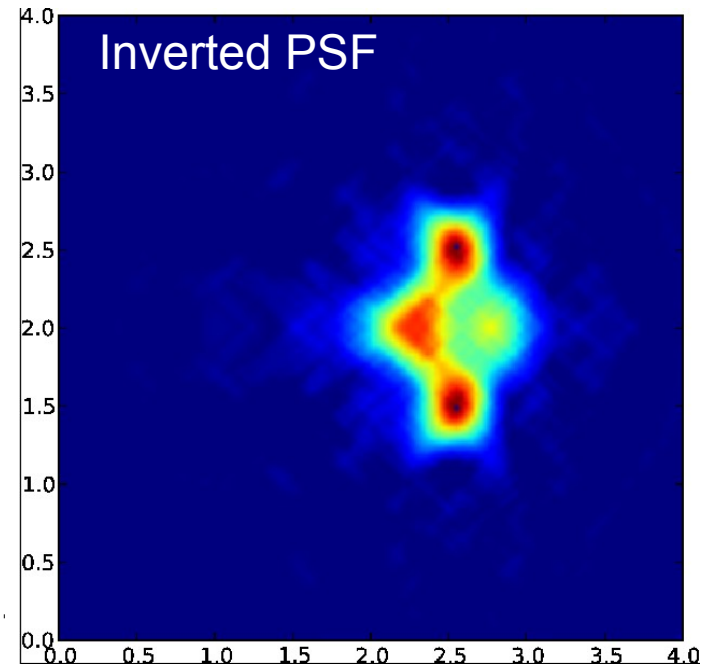
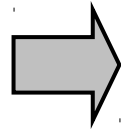
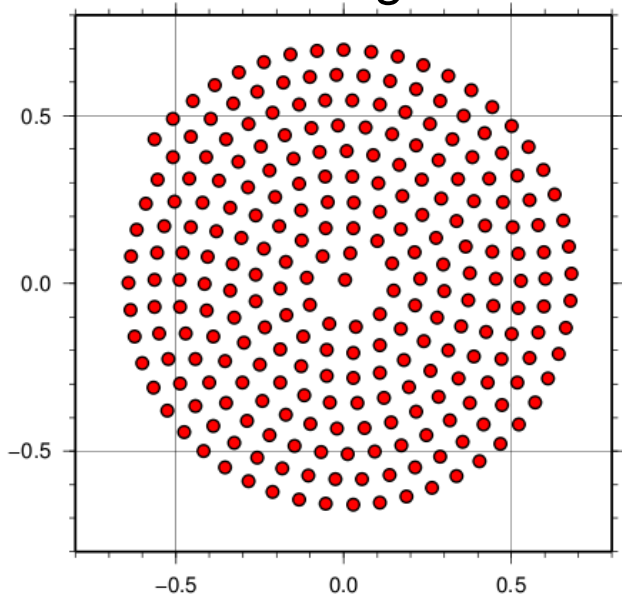
## Assumptions :

- 32 telescopes
- un-correlated noises between telescopes



# PSF modeling

Microscanning



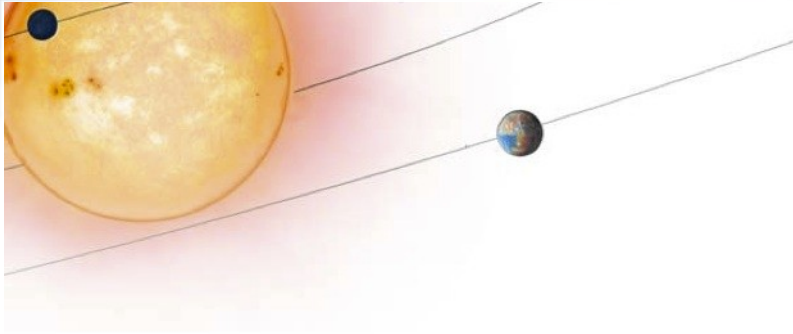
Surface for jitter correction

# Results after jitter correction

	Total	Photo n noise	Photon noise + 1/3	Contam inants	Read- out	Sky backgrou nd
Magnitude range	ppm/ hr	ppm/h r	ppm/hr	ppm/hr	ppm/hr	ppm/hr
9.00- 9.50	<b>14.7</b>	12.8	13.5	0.3	2.7	2.3
9.50-10.00	<b>17.8</b>	16.2	17.1	1.0	4.2	3.5
10.00-10.50	<b>22.5</b>	20.4	21.5	1.5	6.7	5.7
10.50-11.00	<b>29.1</b>	25.5	26.9	2.2	10.5	8.9
11.00-11.50	<b>37.0</b>	32.0	33.7	3.2	16.4	13.8
11.50-12.00	<b>51.9</b>	40.9	43.1	5.0	26.9	22.7

- At  $V=11.25$  we are slightly **ABOVE 1/3** of the photon noise
- Important contribution of the **read-out noise** (here  $68e^-$ ) and **sky-background** ( $150 e^-/s/pixel$ )
- Better **mask parameters** must lead to slightly better performance





# PLATO: instrument performance

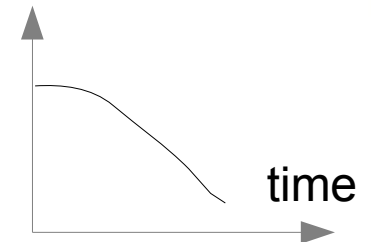
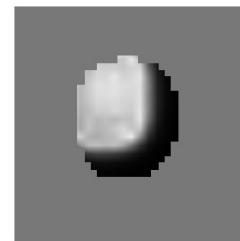
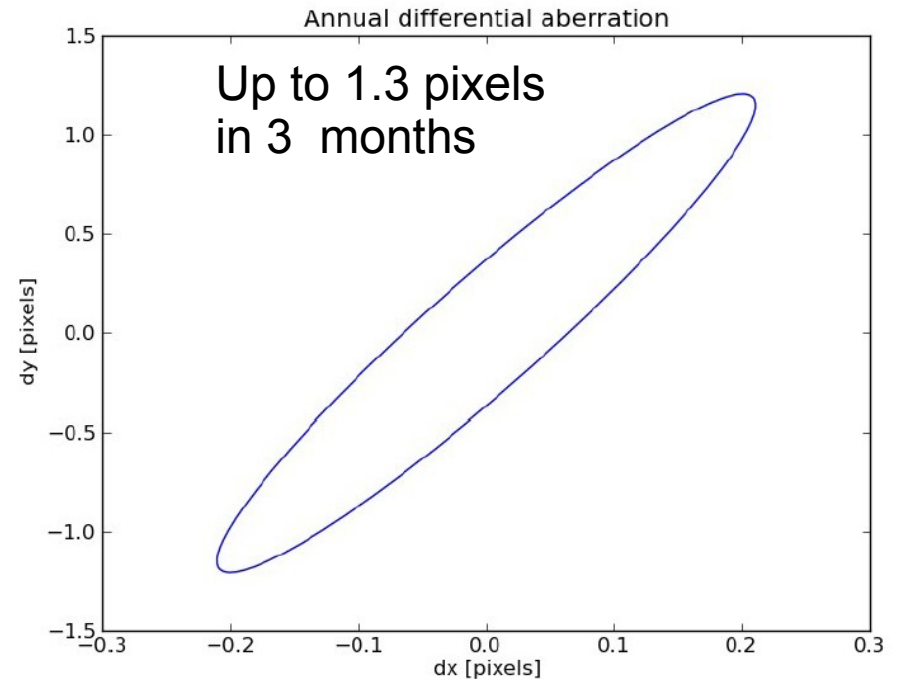
- 1) Noise level requirements
- 2) Expected white noise level
- 3) **Long-term drift**



# Long-term drift

Origins :

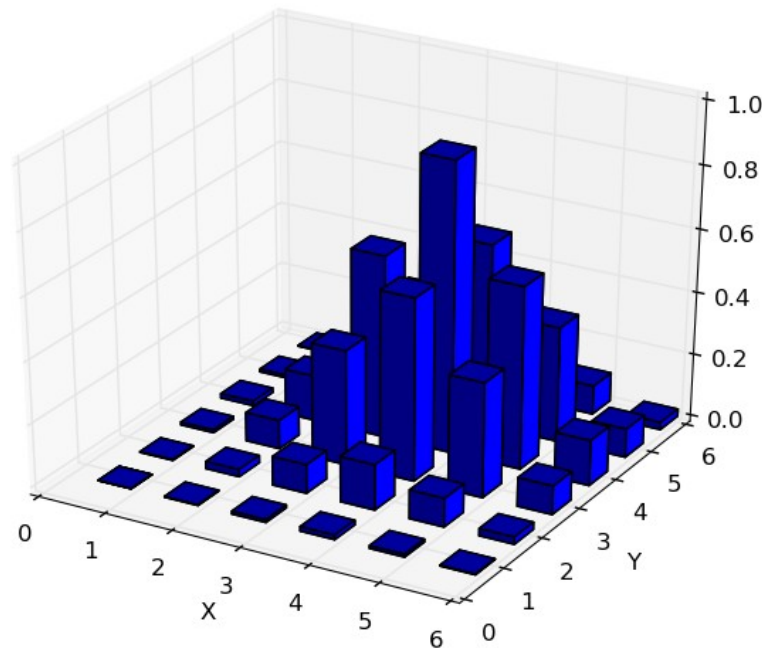
- **Kinematic** aberration
- **Thermoelastic** variation of the pointing direction of a given telescope :
  - Thermoelastic variations of the **telescope structure**
  - Thermoelastic variations of the **platform structure**



# Weighted mask

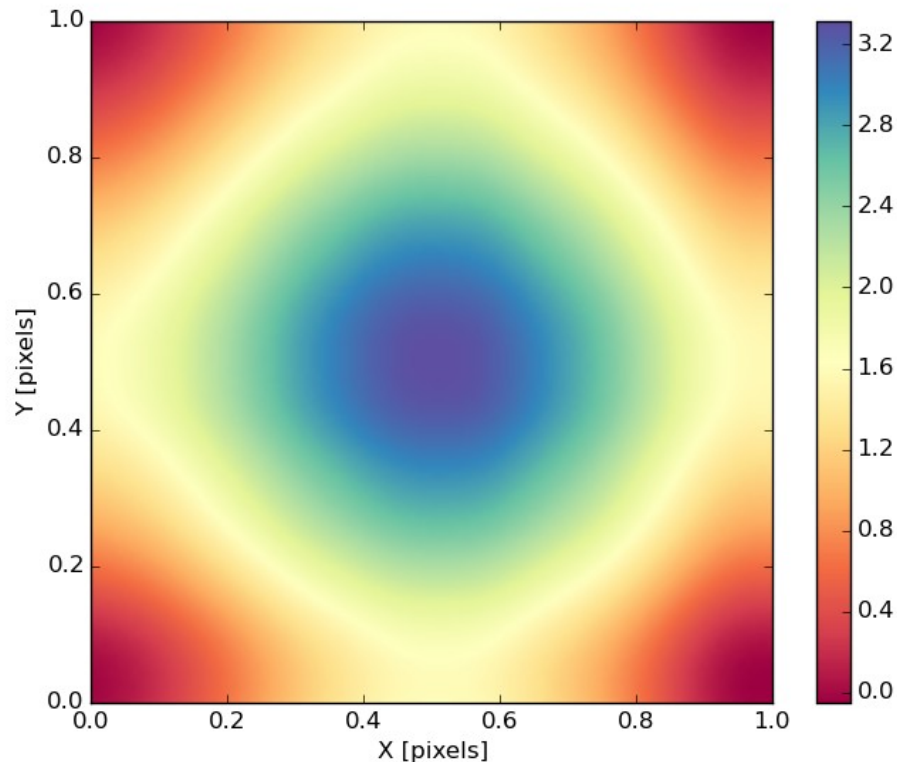
Illustrative case of a *Gaussian* mask:

$$M(x_i, y_i) = \exp \left[ -\frac{1}{2} \left( \left( \frac{x-x_0}{\sigma_x} \right)^2 + \left( \frac{y-y_0}{\sigma_y} \right)^2 \right) \right]$$



# Mask update

## Residual flux variation

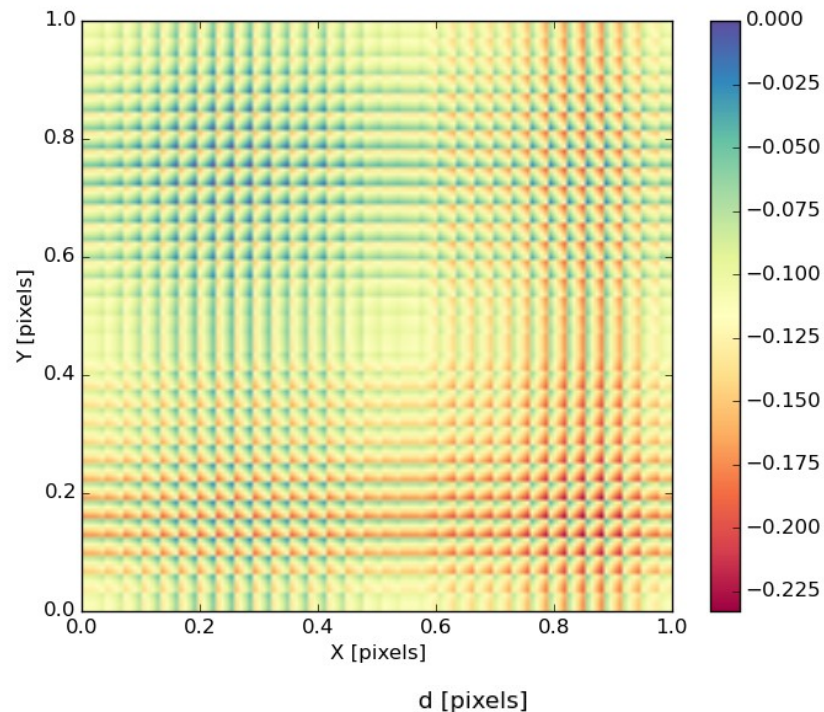


- Gaussian mask updated every 1/128 pixels (resolution of the PSF)
- Residual of the order of  $\sim 3\%$  (worst case → edge of the FoV)
- Can be corrected as we do the **jitter correction using a PSF model**

PSF : at  $18.4^\circ$  ; mask width : 1.6 pixels

# Mask update

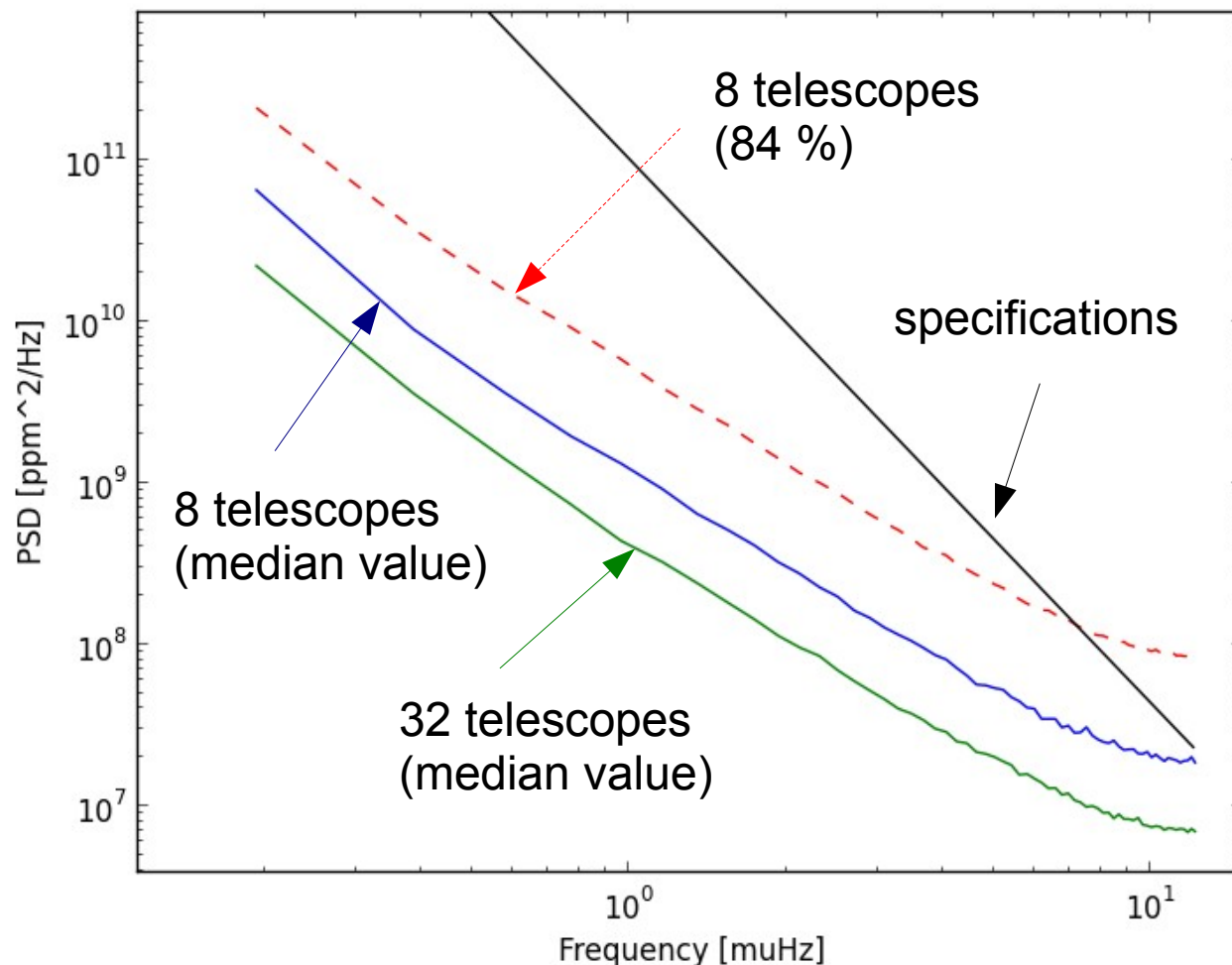
## Residual after (on-ground) correction



- The mask update leaves a variation of up to  $\sim 3\%$  (**worst case**)  $\rightarrow$  edge of the FoV)
- Correction using theoretical **PSF** (resolution of  $1/32$ ) reduce the variation to  $\sim 0.2\%$  peak-to-peak and dispersion of  $0.05\%$  rms
- Residuals **uncorrelated** between telescopes

- Correction efficiency **strongly depends on the quality of the PSF model**
- Can also be reduced if we **change adequately the width and shape of the weighted mask**

# Mask update : residual in the Power Spectral Density



- PRNU included : 0.8 % rms
- Error in the **knowledge** of the PRNU : 0.3 % (rms)

**Thank you !**

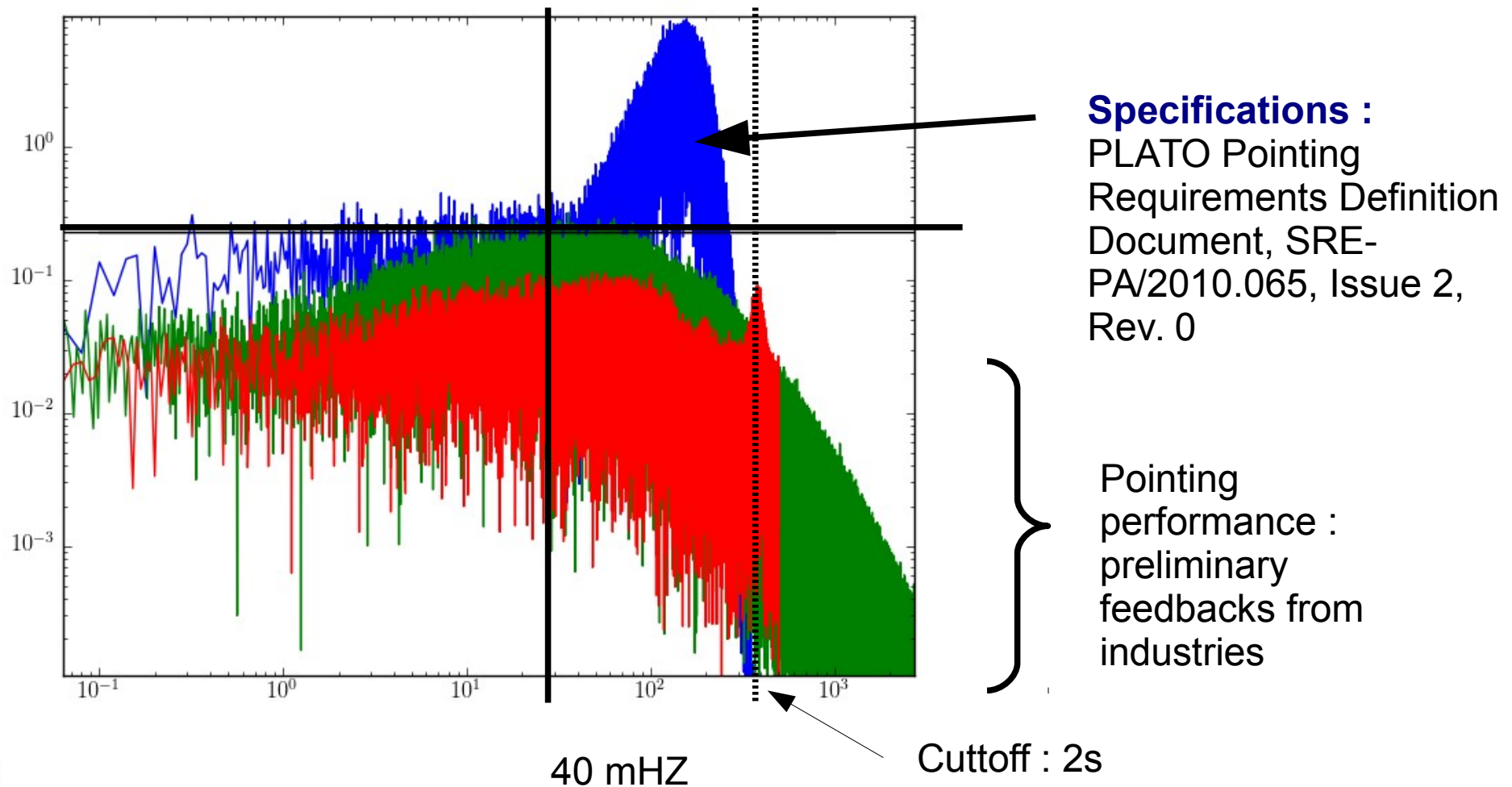


# Jitter noise and PRNU

Magnitude range	With PRNU			No PRNU			No jitter
	Raw NSR ppm/hr	Jitter correction ppm/hr	Correction efficiency ppm/hr	Raw NSR ppm/hr	Jitter correction ppm/hr	Correction efficiency	
9.00- 9.50	25.2	14.9	86.6	24.4	13.8	95.5	13.3
9.50-10.00	29.2	18.8	86.0	29.1	17.6	95.8	17.1
10.00-10.50	32.7	23.3	88.7	33.2	22.3	98.2	22.1
10.50-11.00	37.9	29.2	92.6	37.4	28.6	98.9	28.5
11.00-11.50	44.0	37.5	94.2	43.8	36.7	106.0	37.1
11.50-12.00	56.8	51.3	69.6	56.6	50.9	74.0	48.9
12.00-12.50	74.0			74.5			69.2
12.50-13.00	103.2			102.6			99.1
13.00-13.50	150.9			150.8			140.5
13.50-14.00	215.4			216			208.8
14.00-14.50	327.1			325.1			310.5
14.50-15.00	518.8			518.5			480.7

- **PRNU** has a **negligible** contribution
- Very efficient jitter correction (at least up to  $V < 12$ )
- **Inverted** PSF almost as efficiency than true ones
- Intra-pixel sensitivity (IRNU) : not yet assessed

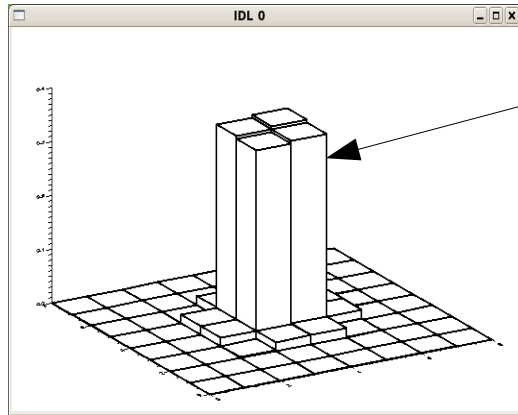
# Satellite jitter : constraints from Industries



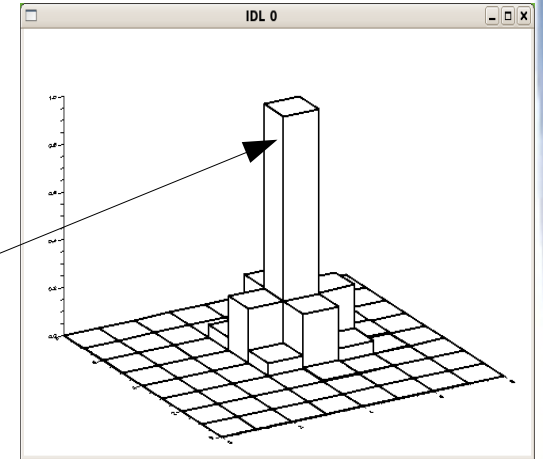
Magnitude	NSR Spec. jitter	NSR Industry	No Jitter	NSR Photon noise
9.00- 9.50	24.1	13.2	13.2	12.8
9.50-10.00	28.8	16.7	16.5	16.1
10.00-10.50	32.9	21.5	21.5	20.5
10.50-11.00	39.2	28.4	28.0	25.6
11.00-11.50	45.3	37.7	37.6	32.2
11.50-12.00	58.4	51.3	51.1	40.5
12.00-12.50	77.4	70.9	70.8	50.8
12.50-13.00	109.1	103.9	103	64.2
13.00-13.50	165.9	157.3	156.2	82
13.50-14.00	244.2	235.2	231.2	103.3
14.00-14.50	374.5	358.9	354.8	129
14.50-15.00	571.6	542.8	539.4	161.6

→ Much **lower**  
NSR with  
satellite jitter  
given by the  
industries

# Saturation limit : N-camera



20% of  
the flux

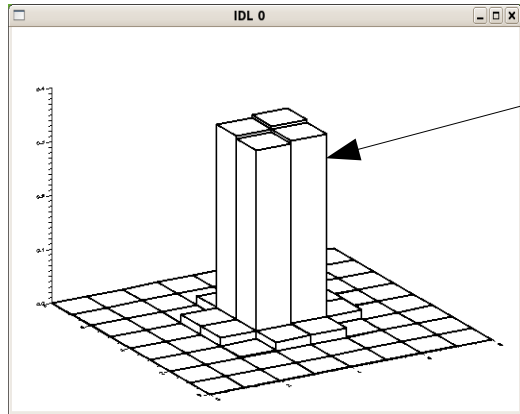


70 % of  
the flux !

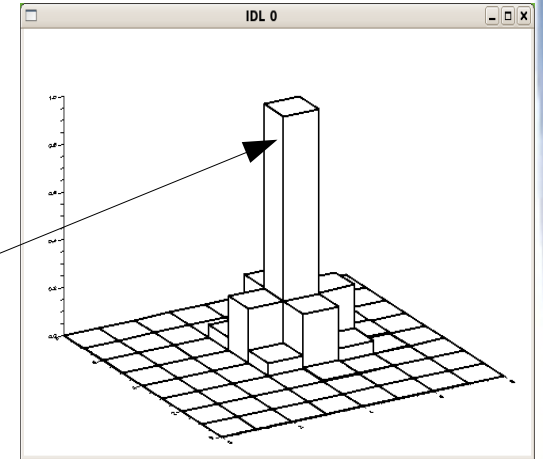
Transmission	P0 [mag]	P1 [mag]	P2 [mag]	P3 [mag]
1% coating	8.35	8.96	8.86	9.51
2% coating	8.21	8.82	8.72	9.37

For more details see PLATO-DLR-PL-TN-003

# Saturation limit : F-camera



20% of the flux

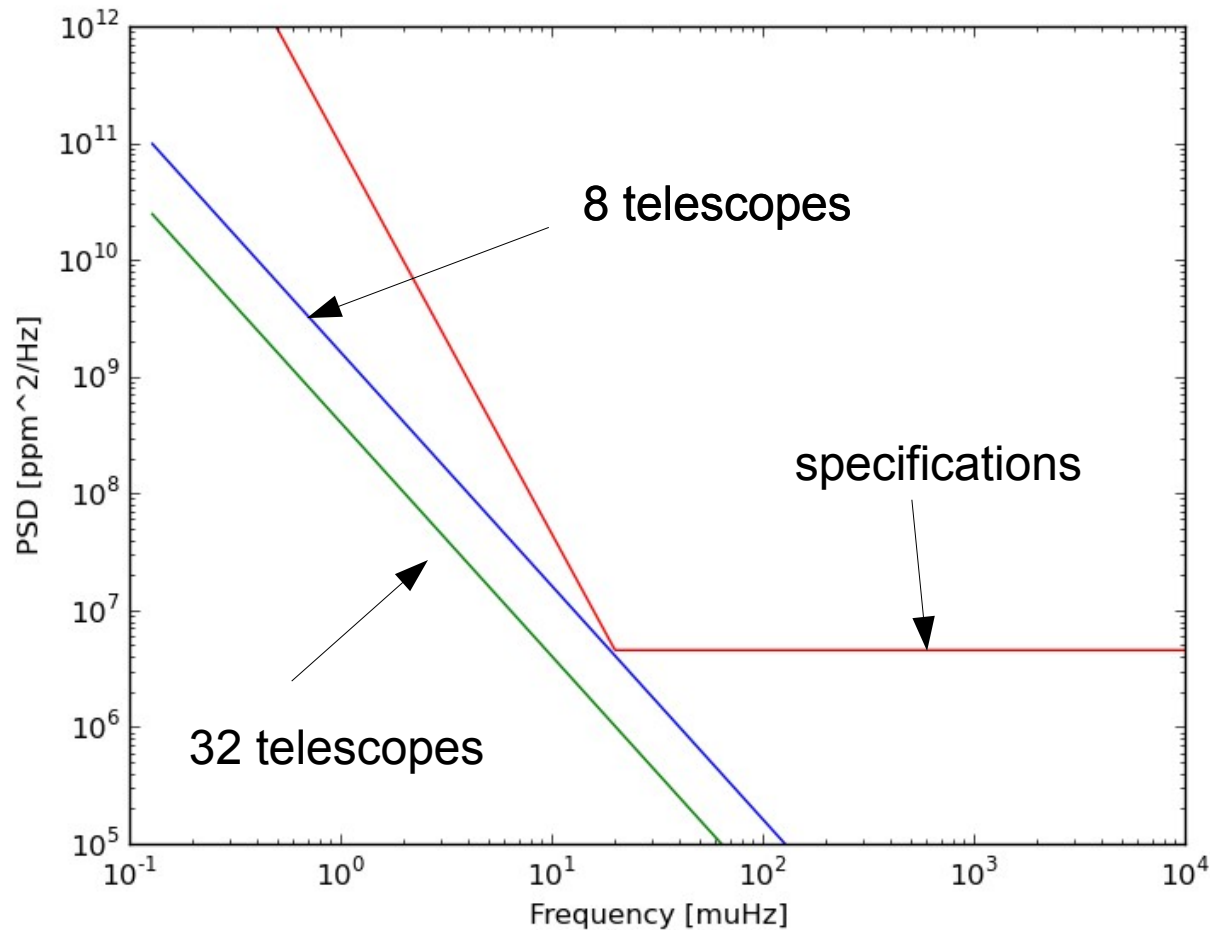


70 % of the flux !

Transmission	Filter	P0 [mag]	P1 [mag]	P2 [mag]	P3 [mag]
1% coating	blue	5.23	5.84	5.73	6.38
	red	4.94	5.55	5.45	6.09
2% coating	blue	5.09	5.70	5.59	6.24
	red	4.80	5.41	5.30	5.95

For more details see PLATO-DLR-PL-TN-003

# Mask update : residual in the Power Spectral Density



Residual :

- assumed to be a linear variation of  $\sim$  **0.2 %** in **3 months** (for one telescope)
- **uncorrelated** between telescopes

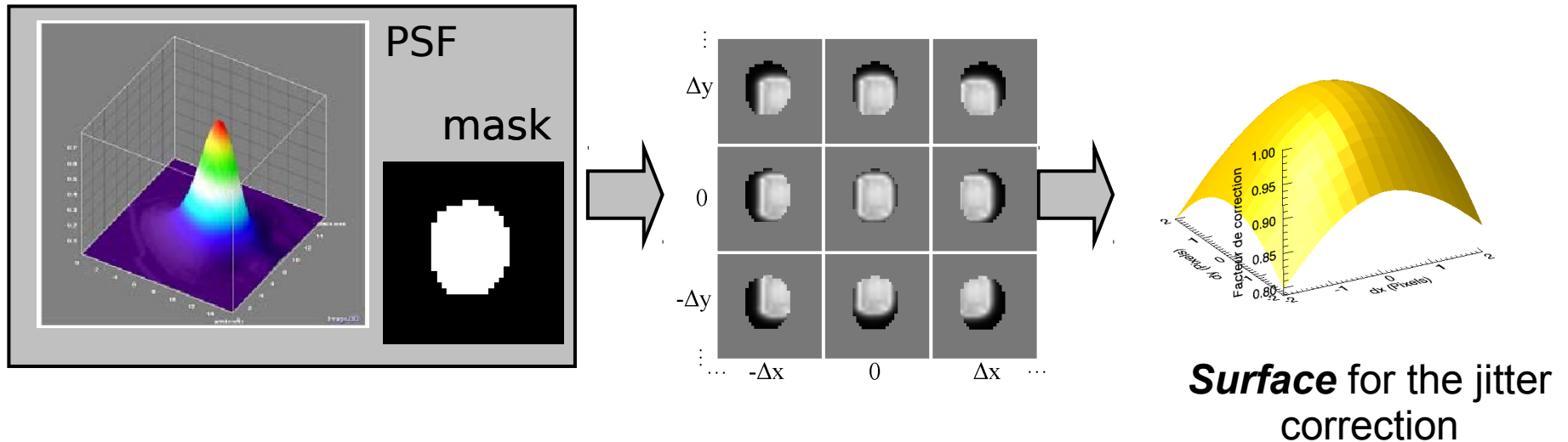


# Raw results

Magnitude	NSR 10 %	NSR 50%	NSR 90 %	NSR Photon noise
9.00- 9.50	15	24.1	37	12.8
9.50-10.00	20.9	28.8	40.5	16.1
10.00-10.50	24.8	32.9	44.8	20.5
10.50-11.00	30.9	39.2	49.9	25.6
11.00-11.50	38.4	45.3	55	32.2
11.50-12.00	50.6	58.4	70.3	40.5
12.00-12.50	67.1	77.4	93.9	50.8
12.50-13.00	90.3	109.1	194.3	64.2
13.00-13.50	133.6	165.9	688.9	82
13.50-14.00	197.4	244.2	620.7	103.3
14.00-14.50	288.3	374.5	1318.8	129
14.50-15.00	447.9	571.6	1486.8	161.6

# Jitter correction

WP 325 100 : F. Fialho



› Thanks to a PSF model, we can predict the perturbations induced by any displacements :

Fialho et al (2007, PASP)

- › Also corrects the **long-term drifts**
- › Require accurate star [displacements](#) ( $\Delta x$ ,  $\Delta y$ ) as well as [PSF](#) !
- › The surface correction must take into account the [presence of contaminants](#)
- › [GAIA](#) : [positions](#) and [intensities](#) of the contaminants [known a priori](#)

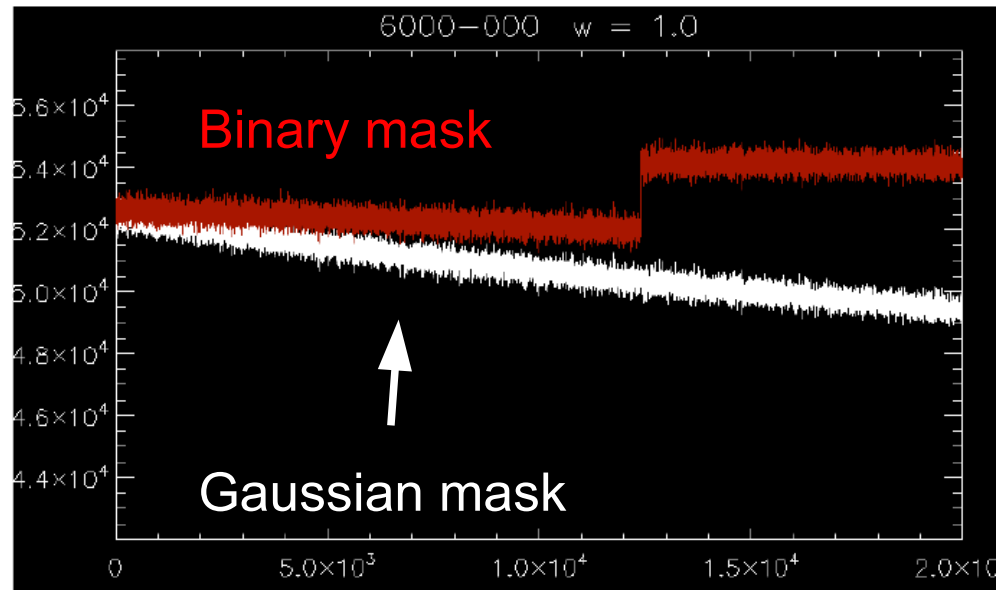
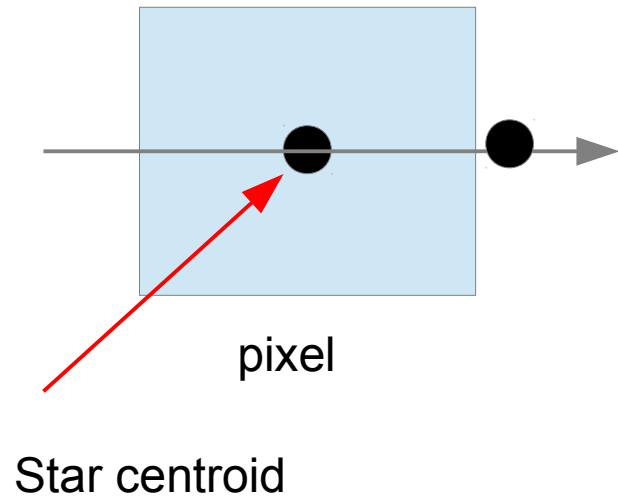
# Global performance assessment

For further details see :

- Phase A – assessment study, PLATO-GS-TN-235-LESIA, December 2011
- Phase B1 - assessment study, PLATO-LESIA-PDC-RP-0012, November 2014
- Estimation of the correlated noise induced by the satellite jitter, PLATO-LESIA-PDC-TN-012, February 2015

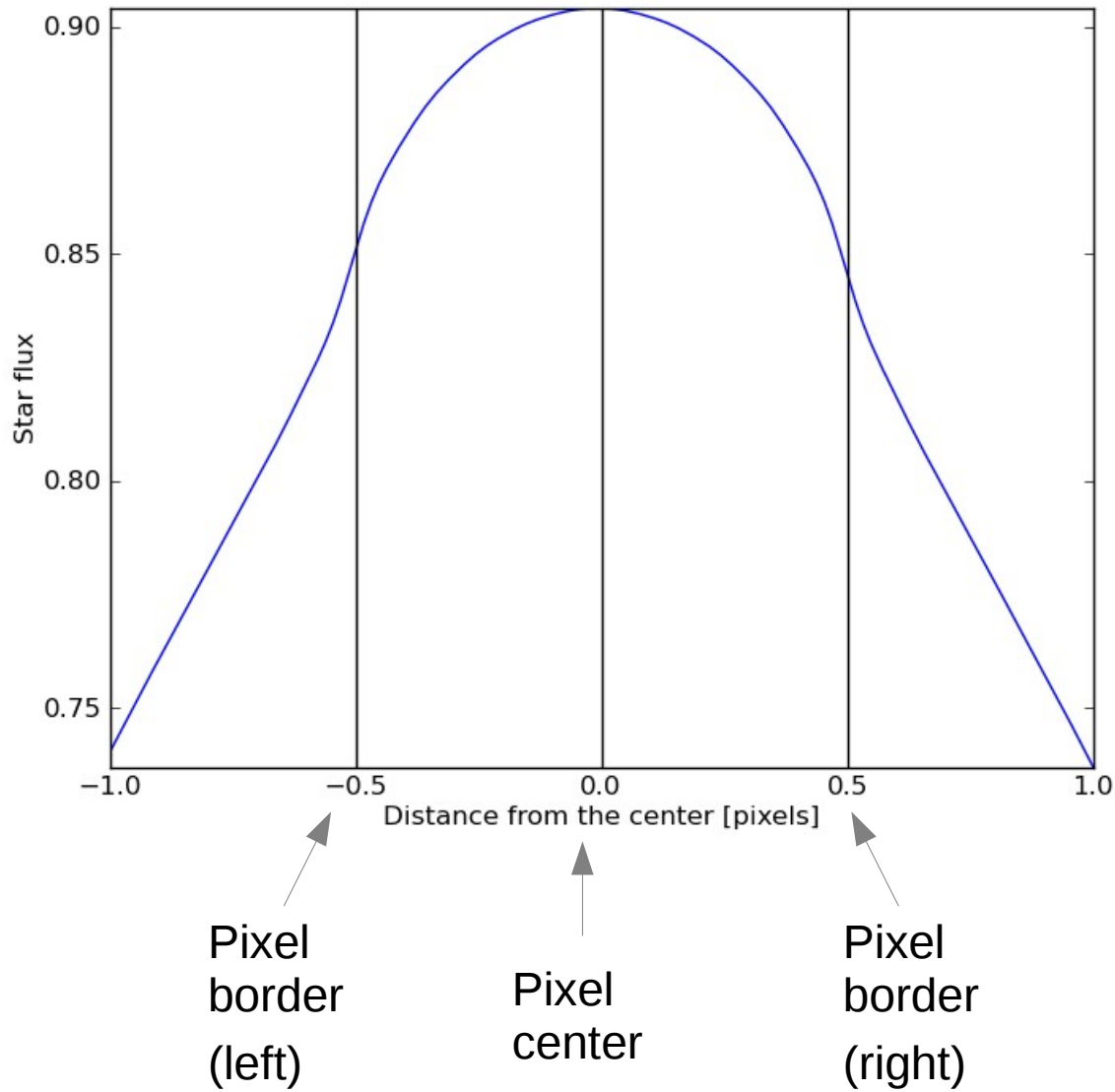
# Binary mask or weighted mask ?

1 pixel = ~ 70 days



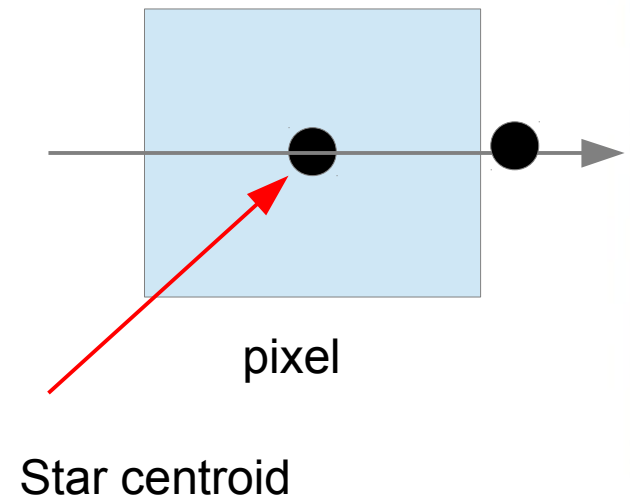
(credit : M. Auvergne)

# Long-term drifts



Gaussian weighted mask centered in the middle of a pixel

1 pixel = ~ 70 days



# Mask updates : how to proceed ?

$$M(x, y) = F(x - x_0, y - y_0)$$

$(X_0, Y_0)$  : star centroid at a given instant

$$x_0 = f(t) \quad y_0 = g(t)$$

→ The mask is computed on the basis of an analytical function (e.g. Gaussian)

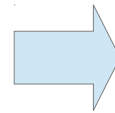
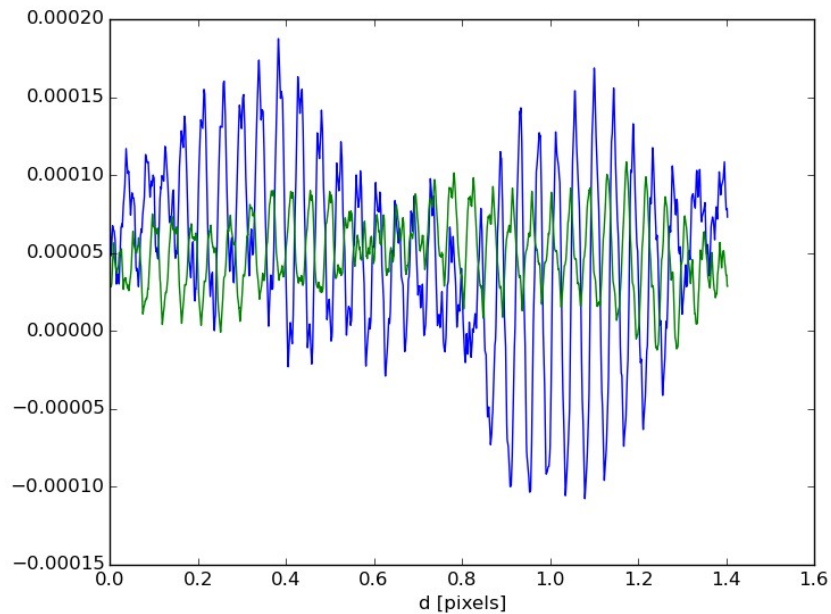
The star centroid  $(x_0, y_0)$  moves due to:

- The **kinematic differential aberration** → *fully predictable*
- The **movements of the satellite** (jitter) → corrected a posteriori on-ground
- The **thermoelastic differential aberration** → regular update of the attitude calculation : on board ?

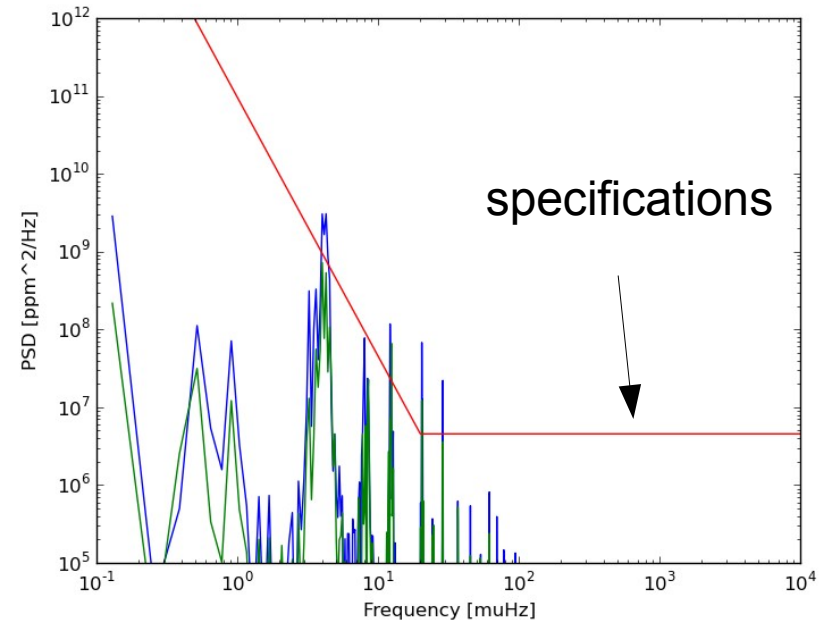


# Mask update : residual in the Power Spectral Density

Residual after (on-ground) correction



PSF 1/32 pixels  
Residuals un-correlated btw telescopes



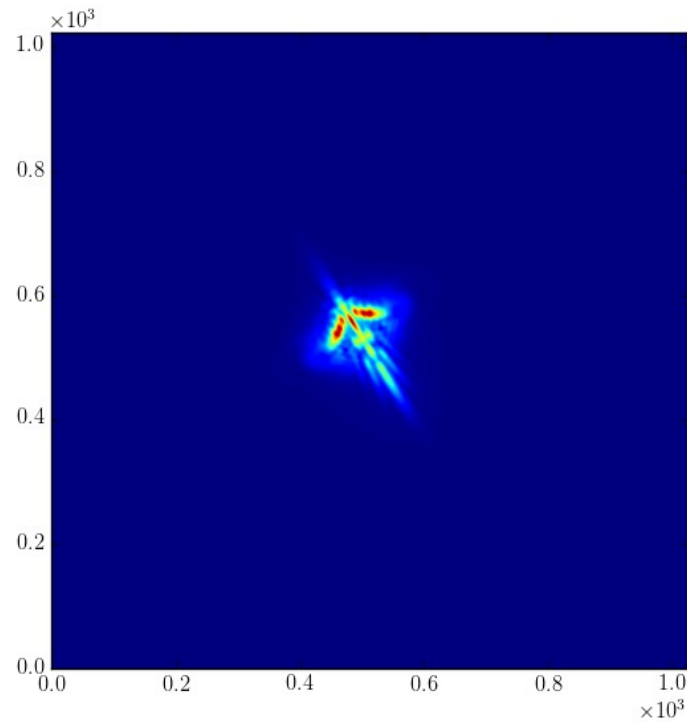
Peaks will be lower :

- Long-term drifts are not linear in time
- Sampling effects can be reduced (eg. interpolation of the PSF)

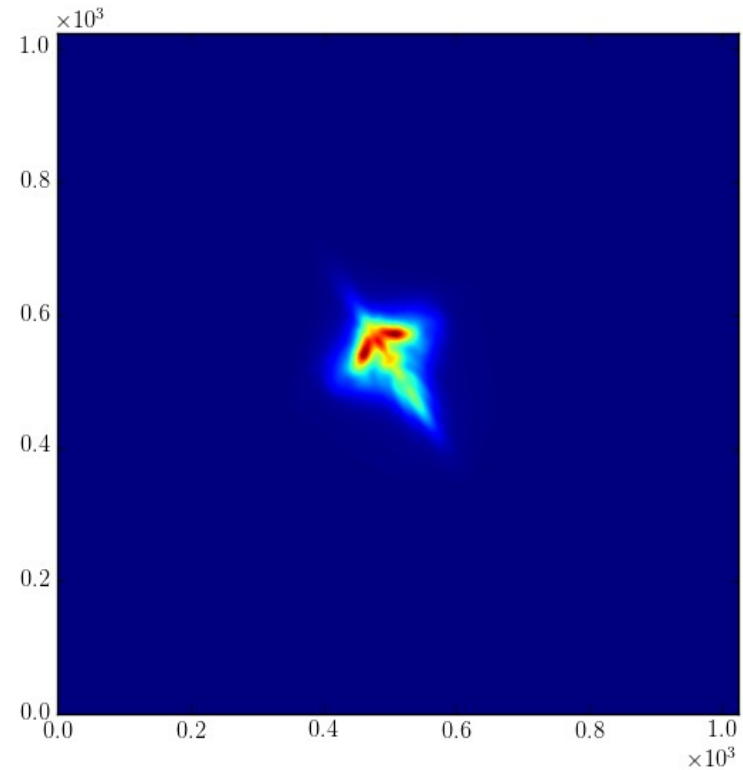
# Open issues (among others...)

- **PSF modeling:**
  - Feasibility of the microscanning to be further studied
  - All sources of error must be taken into count
  - PSF breathing to be quantified and modeled
- **Jitter correction:**
  - Correlated noise to be included in performance calculations
  - All sources of error must be taken into count
  - Constraints on the positions and amplitudes of contaminants ?
- **Photometry:**
  - Optimal adjustement of the mask shape and size
- **Attitude estimation and calibration of the field of view model** (eg. optical distortion):
  - Accuracy ?
  - Frequency ?
  - On board ?

# PSF blurring



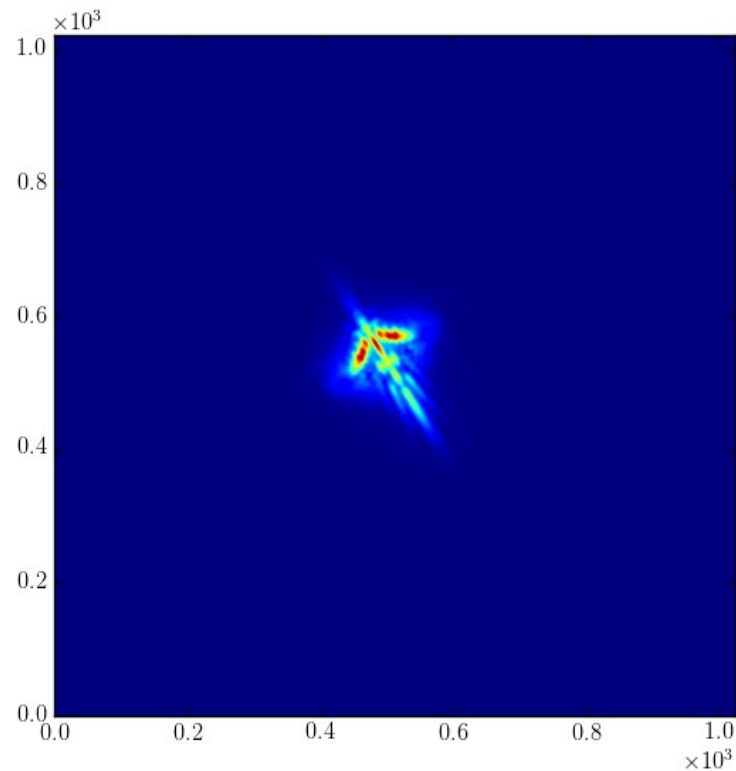
Original **PSF**



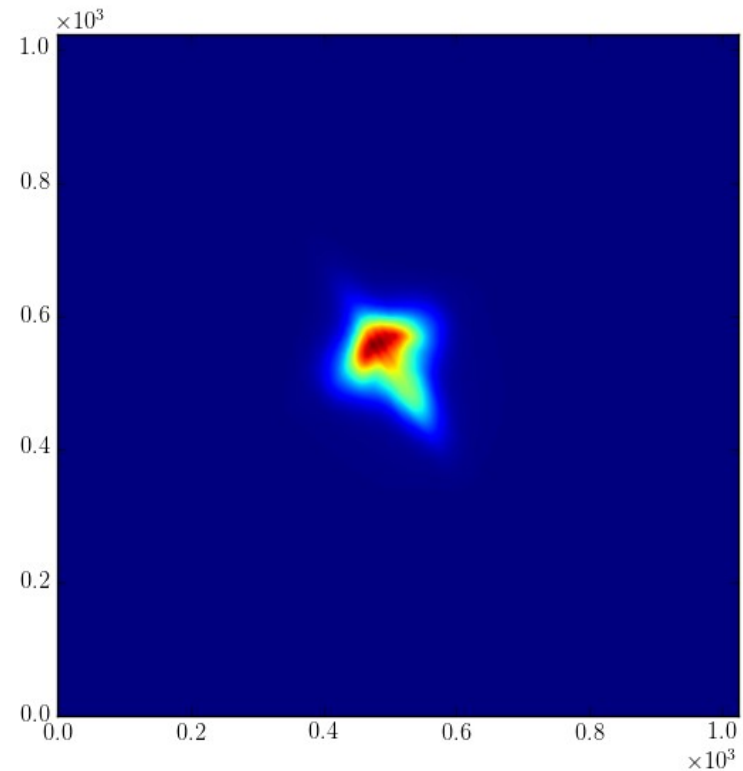
Blurred **PSF**  
Cutoff : **2** seconds

- ➔ Blurring (due to movements shorter than 2.2s) has a low impact on the performance
- ➔ The model of blurring must be consolidated

# Blurring due to the integration time



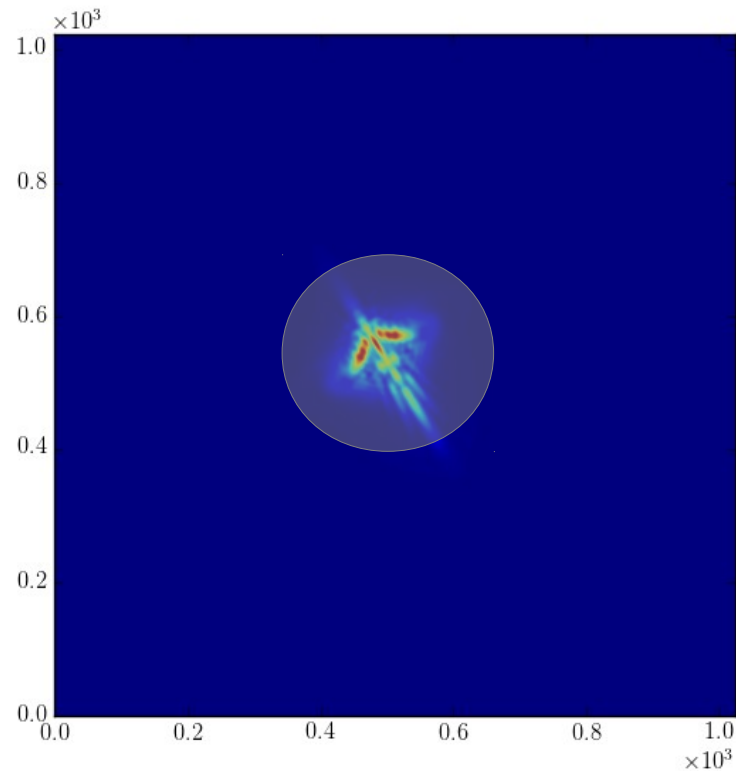
Theoretical **PSF**  
(instantaneous)



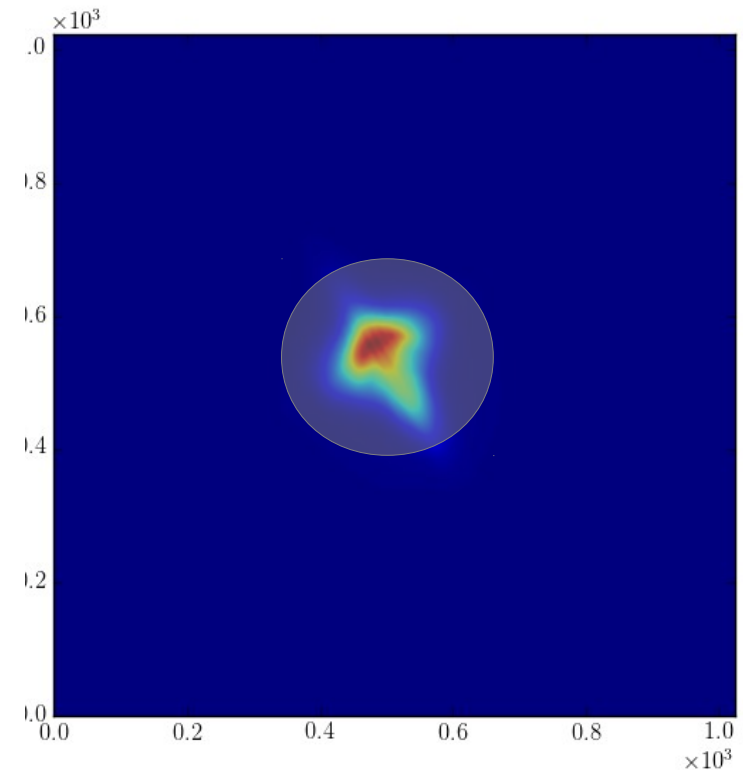
Blurred PSF with **specified jitter**  
**22 seconds integration time**

# Blurring due to the integration time

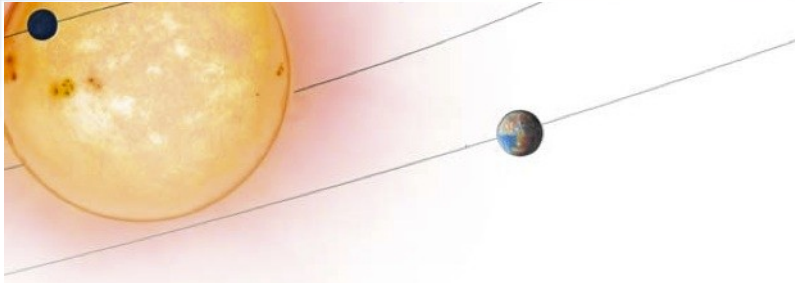
22 seconds integration time



Blurred PSF with **Airbus jitter**



Blurred PSF with **specified jitter**



# Data Processing Algorithms

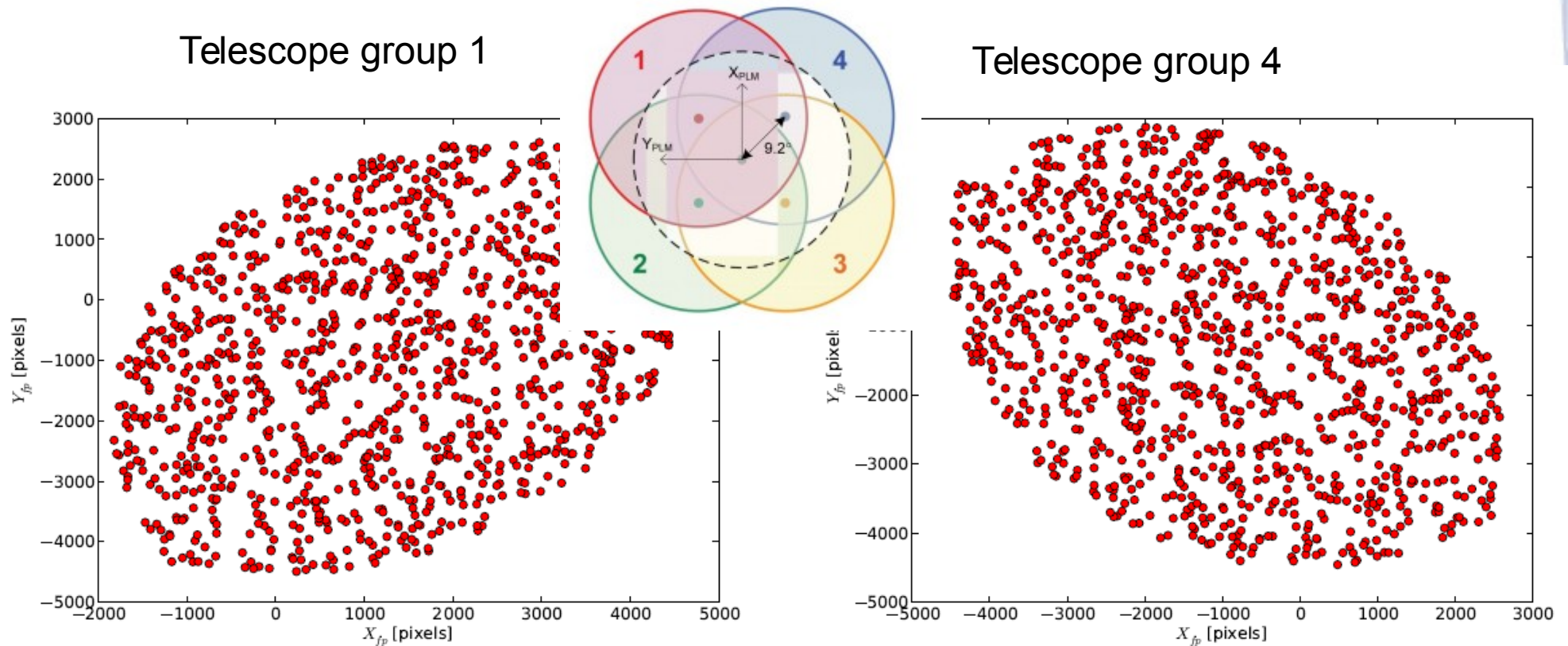
## Pointing meeting

- 1) Photometric perturbations induced by satellite jitter
- 2) Photometry performance assessment
- 3) **Correlated noise induced by satellite jitter**
- 4) Long-term drift



# Correlated noise and satellite jitter

- Two telescopes simulated with PIS
- About 1200 imagettes centred around targets common to the 2 telescopes

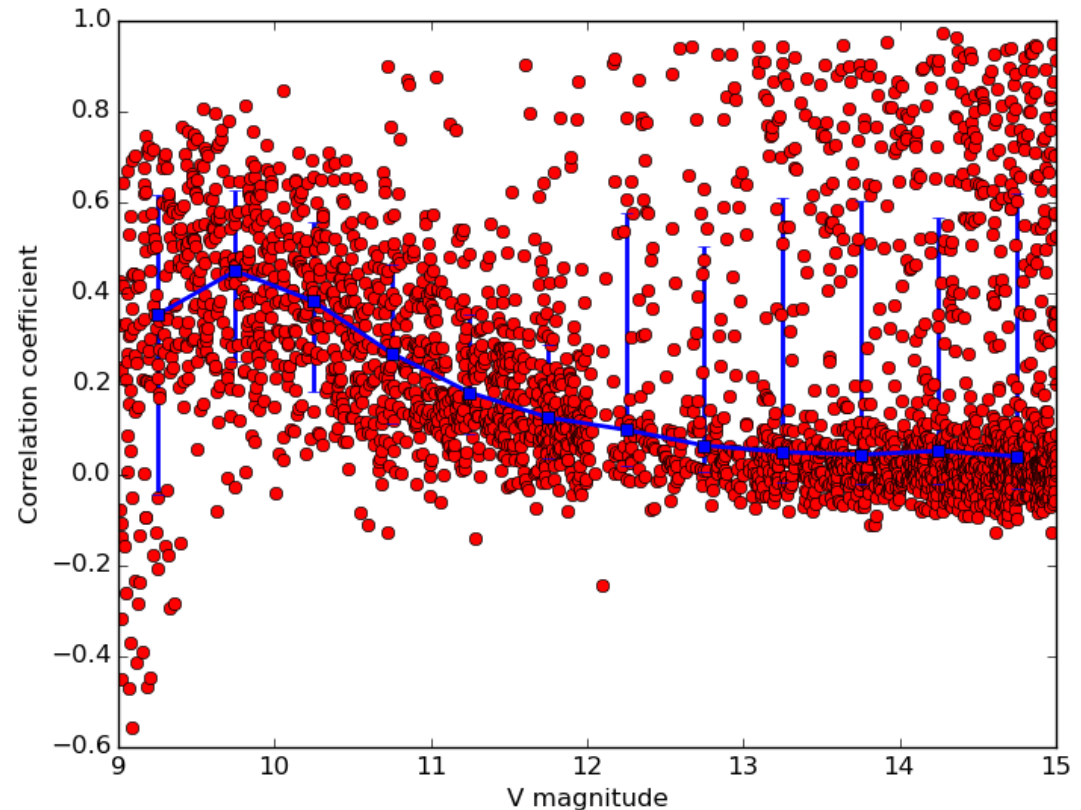


# Correlated noise and satellite jitter

Correlation coefficient :

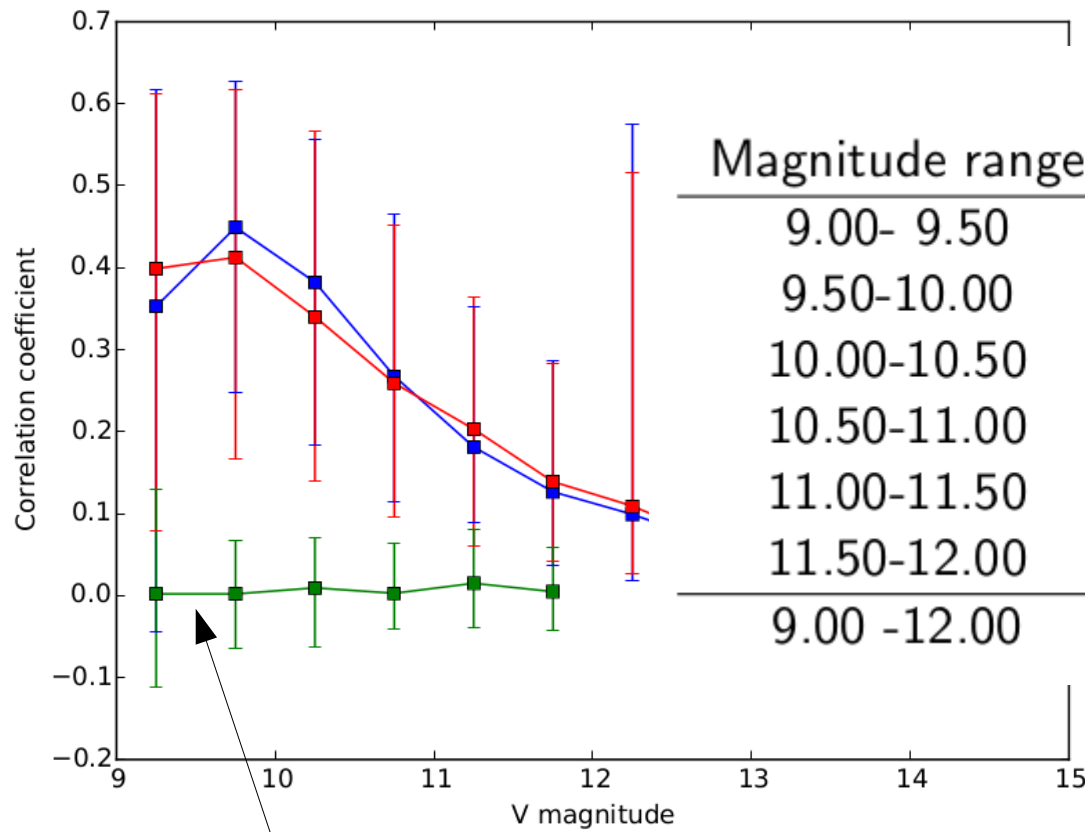
$$c_{X,Y} = \frac{\overline{(f_X - \overline{f_X}) (f_Y - \overline{f_Y})}}{(\text{Var}(f_X) \text{Var}(f_Y))^{1/2}}$$

- High level of correlation
- Strong dispersion
- Correlation coefficient decreases with increasing magnitude because of the decrease of the relative contribution of the jitter noise



→ « *Estimation of the correlated noise induced by the satellite Jitter* », PLATO-LESIA-PDC-TN-012

# Correlated noise and satellite jitter



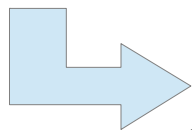
Magnitude range	$C_{A',B'}$		
	16 %	50 %	84 %
9.00- 9.50	-0.112	$0.002^{+0.02}_{-0.01}$	0.129
9.50-10.00	-0.065	$0.002^{+0.01}_{-0.02}$	0.067
10.00-10.50	-0.062	$0.009^{+0.01}_{-0.01}$	0.071
10.50-11.00	-0.041	$0.003^{+0.01}_{-0.01}$	0.064
11.00-11.50	-0.039	$0.015^{+0.01}_{-0.01}$	0.081
11.50-12.00	-0.042	$0.005^{+0.01}_{-0.01}$	0.060
9.00 -12.00	-0.0548	$0.0057^{+0.004}_{-0.004}$	0.0723

Correlation coefficient **after** jitter correction

# Correlated noise and satellite jitter

Noise-to-Signal Ratio (NSR) with correlated noise :

$$NSR = \frac{1}{\bar{y}} \left( \sum_{i \neq j} C_{i,j} \sigma_i \sigma_j + \sum_i \sigma_i^2 \right)^{1/2}$$



$$NSR = NSR_0 \sqrt{1 + (N - 1)C}$$

correcting factor

NSR for un-correlated noise

C = 0.006  
and  
N = 32 telescopes

correcting factor **f** ~ **10 %** ( 5 % for N = 8)

But **large uncertainties** on the determination of C :

- low statistic
- still ideal jitter correction

→ « *Estimation of the correlated noise induced by the satellite Jitter* », PLATO-LESIA-PDC-TN-012

# PLATO noise specifications for asteroseismology (N and F cameras)

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R.Samadi<sup>2</sup>, T.Morel<sup>3</sup>, A.Robin<sup>4</sup>

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2) Observatoire de Paris-Meudon, France

3) Institut d'Astrophysique et de Géophysique, Liège, Belgium

4) Observatoire de Besançon

# Goal of the specification

- Typical flow down approach, i.e. from Science specifications to instrumental specifications
- Need to know the Radius, Mass and Age to 1%, 2% and 10% for thousands of stars of the P1 sample.
- Goal: what is the specification on the noise background in the power spectrum?



# Assumptions for S/N for PLATO (I)

- Application to P1 sample only (worst case): dwarfs and sub-giants later than spectral type F5
- For P1, we have to derive stellar masses, radii and age for thousands of stars
- Radius, mass and age needs precise mode frequencies measured to better than 0.2  $\mu\text{Hz}$
- Mode frequency precision given by Libbecht (1992) as:

$$\sigma_v^2 = f(\beta) \frac{\Gamma}{4\pi T}, \quad (2)$$

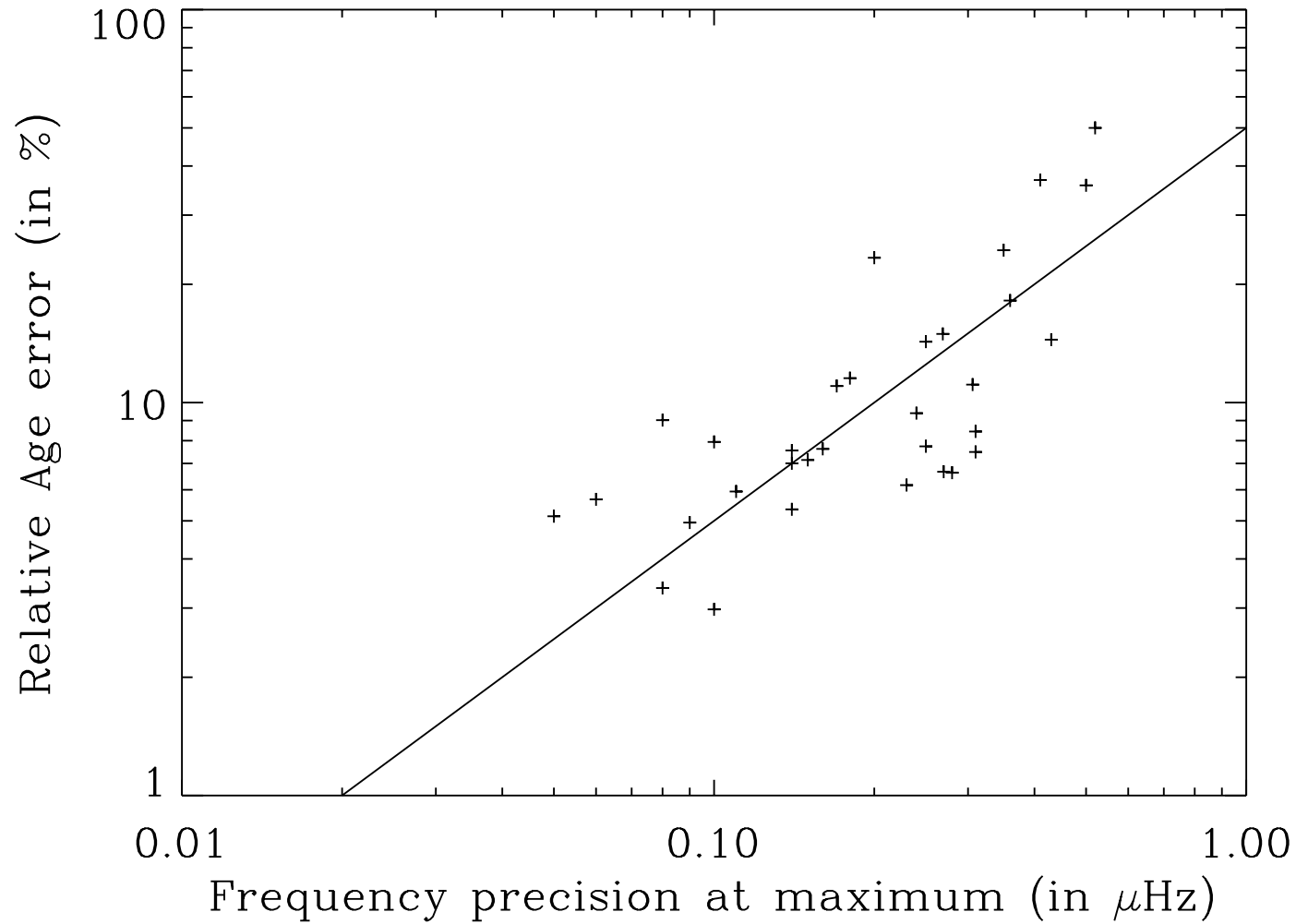
where  $\beta = B/A$  is the inverse signal-to-noise ratio and

$$f(\beta) = (1 + \beta)^{1/2} [(1 + \beta)^{1/2} + \beta^{1/2}]^3 .$$

where  $\Gamma$  is the mode linewidth,  $T$  is the observing time,  $B/A$  is the inverse signal-to-noise ratio in the power spectrum ( $B/A$  is now termed  $B/H$ )

- For a 2-year observing, a mode linewidth of 1  $\mu\text{Hz}$ , a S/N of 1, the mode frequency precision is better than 0.2  $\mu\text{Hz}$

# A naive derivation of age error

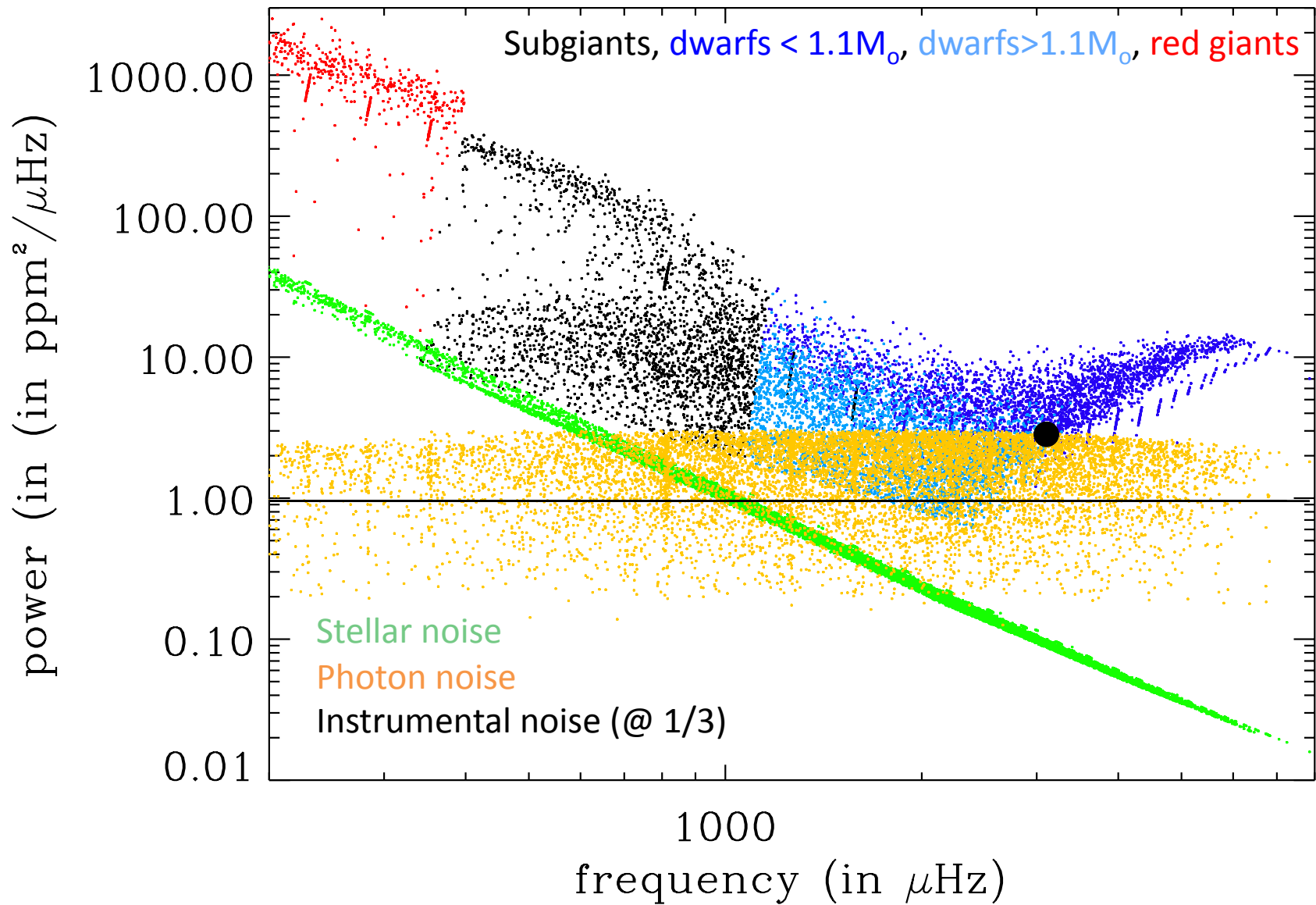


After Metcalfe et al (2014) and  
Appourchaux et al (2012)

# Assumptions for S/N for PLATO (II)

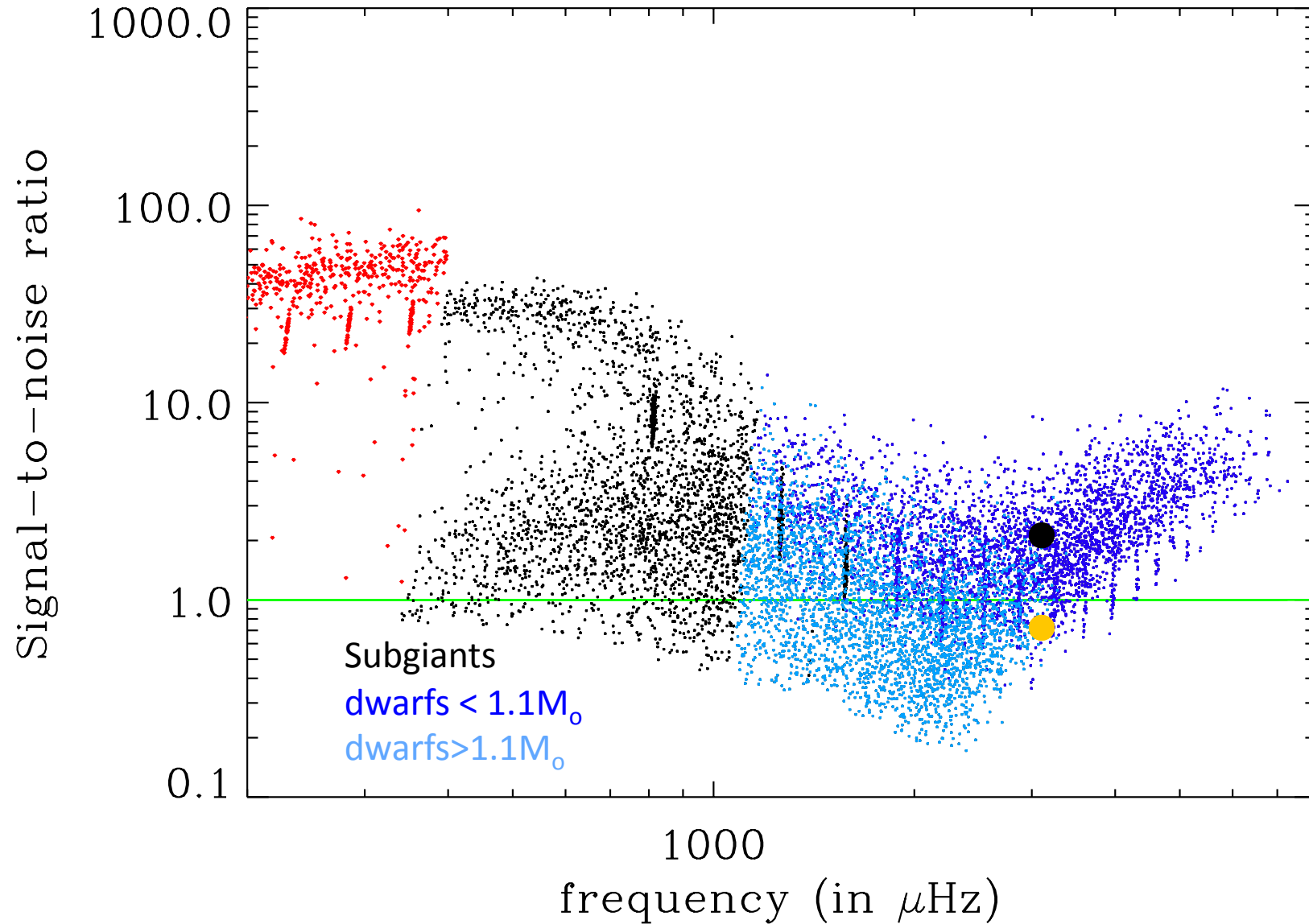
- Mode height ( $H$ ) derived from:
  - Mode amplitude  $A$  from Corsaro et al (2013)
  - Mode linewidth  $\Gamma$  from Appourchaux et al (2012) for solar-like stars and from Corsaro et al (2013) for red giants
  - Both at frequency of maximum power
- Background noise ( $B$ ) derived from the sum of:
  - Granulation noise from Kallinger et al (2014)
  - Photon noise from PLATO-DLR-MIS-LI-002 (28.2 ppm in one hour for  $m_V=11$  @ 6000K)
  - Instrumental noise specified at 1/9 of the photon noise in power (tests performed at 1/9, 1/3 and 1 of the photon noise)
- Simulation of the P1 from the Robin et al (2003) model comprising about 28000 simulated stars
- S/N calibrated with an independent calculation based on the work of Appourchaux et al (2012)

# Simulation for PLATO P1



# Simulation of S/N for PLATO P1

Fraction of stars above detection level=87%



# Results for the P1 sample

Case	Photon noise	Instrumental noise	Stellar noise	$F_{R,M,Age}$ F	$F_{R,M,Age}$ G	$F_{R,M,Age}$ K	$F_{R,M,Age}$ Subgiants	$F_{R,M,Age}$ Giants
Ca	x	1/9	x	13.1%	14.1%	1.2%	14.7%	47.8%
Cb	x <b>N Cameras</b>	1/3	x	9.6%	13.7%	1.2%	14.2%	47.8%
Cc	x	1	x	3.4%	10.4%	1.2%	12.4%	47.8%
Ca	x	1/9	x	5.3%	7.1%	0.8%	10.3%	62.2%
Cb	x <b>F Cameras</b>	1/3	x	3.4%	6.2%	0.8%	9.4%	62.2%
Cc	x	1	x	0.5%	4.5%	0.8%	7.9%	61.6%

More than 4500 stars of F, G, K type



# Summary

- For asteroseismology, the limit of 28.2 ppm per hour has to include all source of noise: instrumental, photon, stellar
- For the P1 sample simulated by the Robin et al model, an instrumental noise at 1/3 of the photon noise in power, we get stellar masses, radii and age for 87% of all stars, for 23% of all stars being either F, G or K stars
- For the P1 sample simulated by the Robin et al model, an instrumental noise at 1/9 of the photon noise in power, the percentages are increased by 4% (91%, 27% respectively).
- The nominal value of 1/9 is provided with a margin of a factor 3. (1/9 to 1/3 in power)
- Limitation of the study:
  - There are very few measurements of mode height above 3500  $\mu\text{Hz}$  which makes the predictive power very small for light stars.
  - Therefore the results for K stars is likely not to be trusted at all.
  - For G stars, about 6 stars out of 10 have a  $\nu_{\text{max}}$  lower than 3500  $\mu\text{Hz}$
  - All F stars have their  $\nu_{\text{max}}$  lower than 3500  $\mu\text{Hz}$
- Document available: PLATO-IAS-SCI-AN-001 V3.2, March 12, 2015